

Analysis of high magnification events on Q2237+0305 A

Astronomical image of a galaxy, likely Q2237+0305 A, showing a central multi-colored source (blue, yellow, red) surrounded by a diffuse, multi-colored (red, blue, green) emission region. The background is dark with scattered stars.

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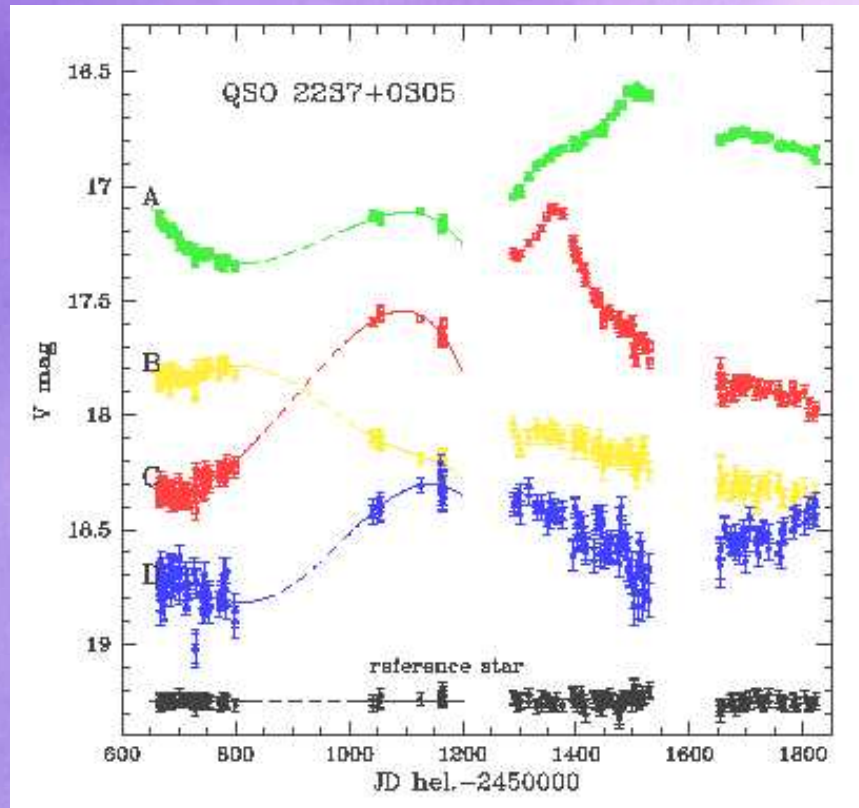
1''

$$z_{\text{LENS}} = 0.04$$

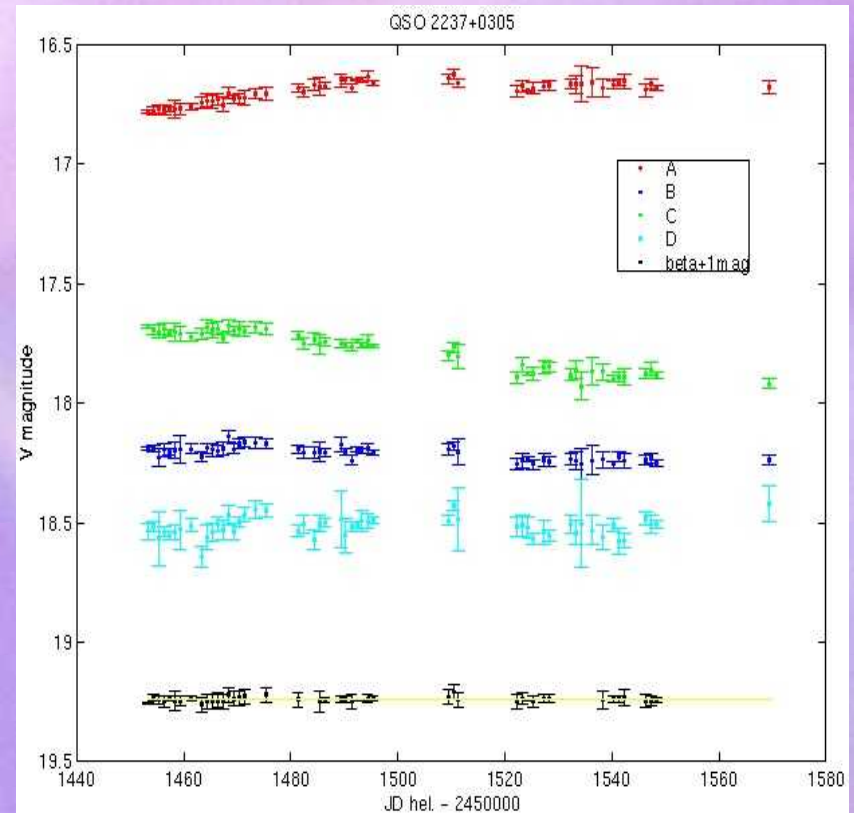
$$z_{\text{SOURCE}} = 1.7$$

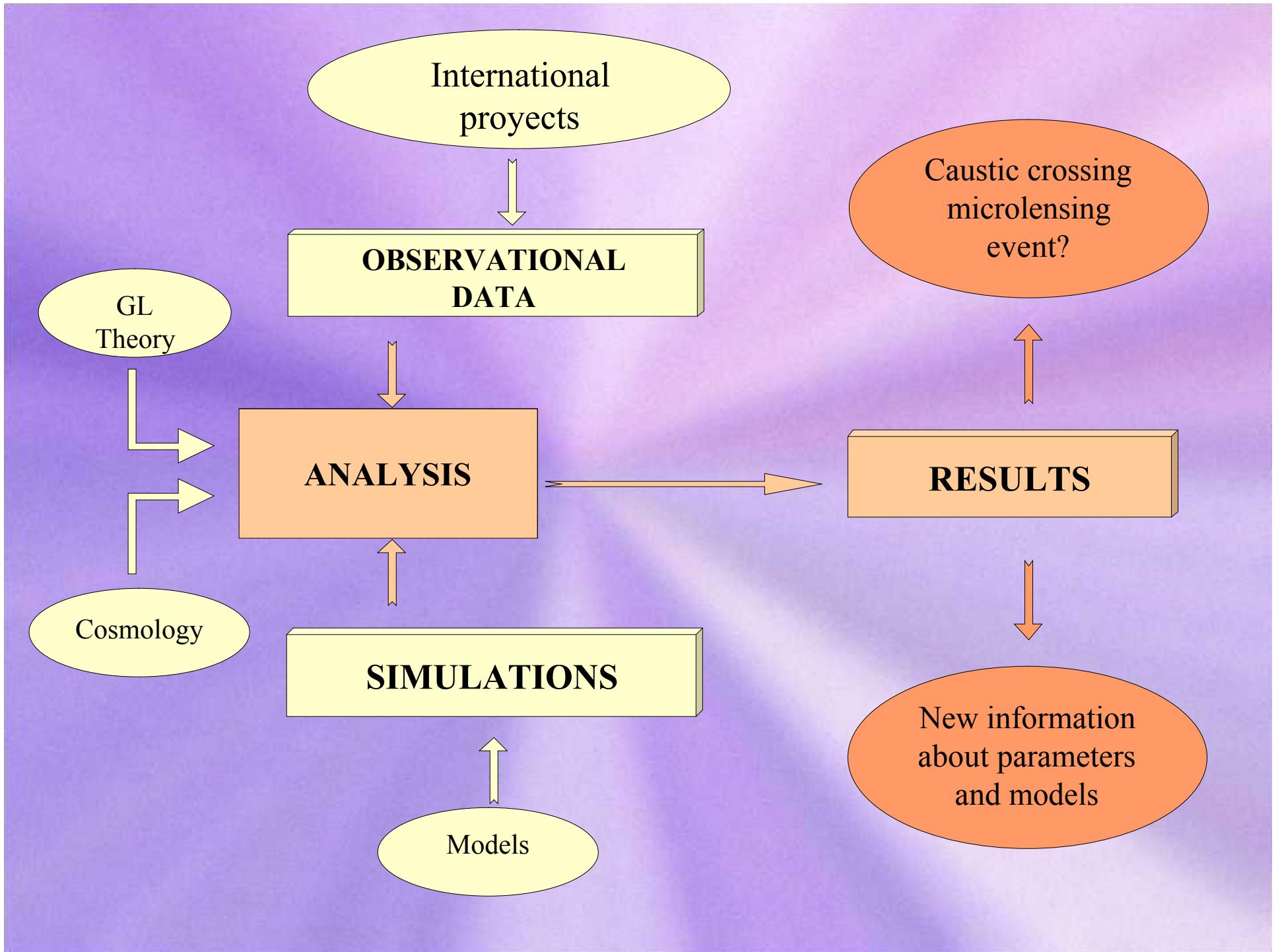
Observational data

OGLE collaboration

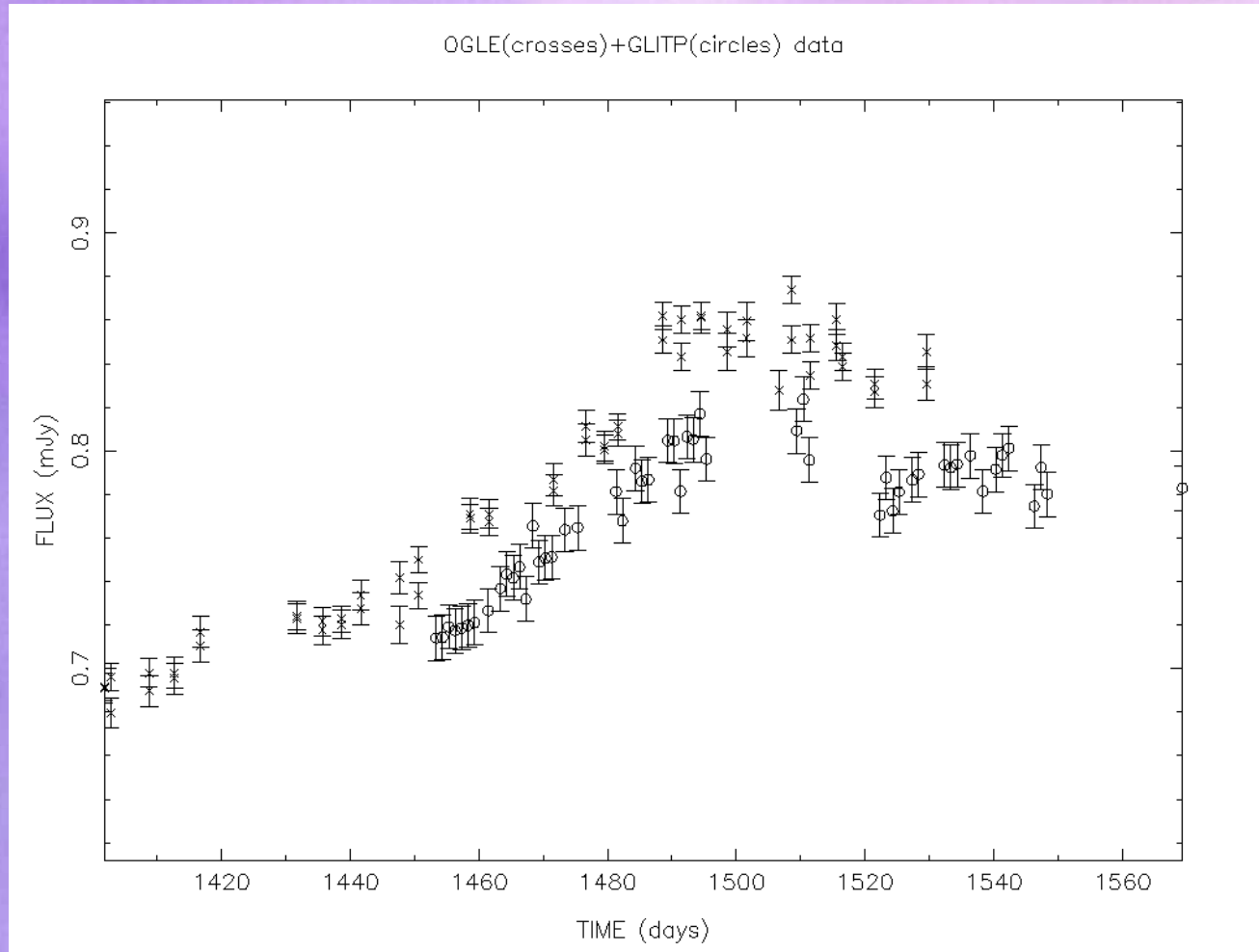


GLITP collaboration





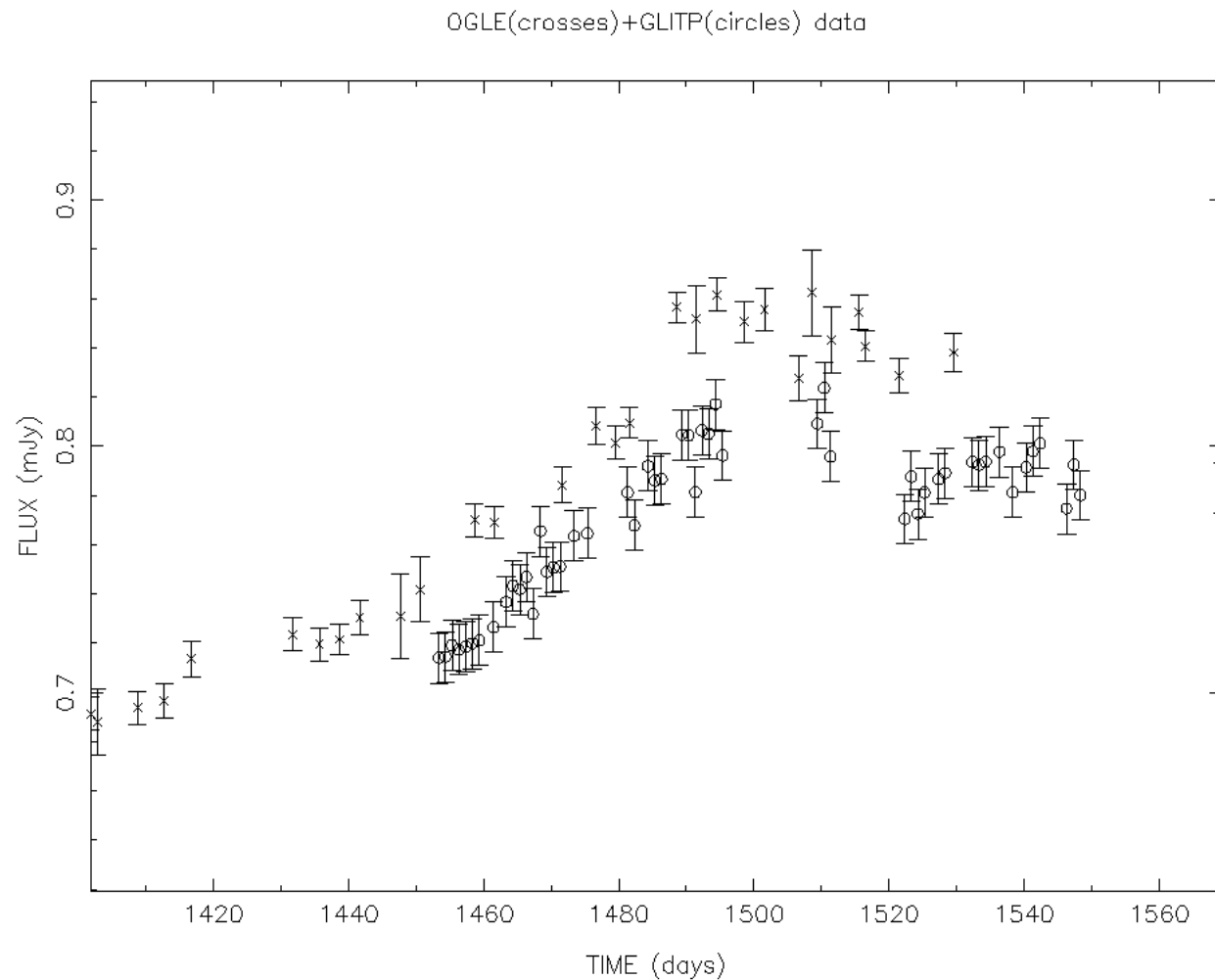
Observational data



Mixture of data I (OGLE+GLITP)

Re-1

$$\bar{t}_i = \frac{\sum_{j=1}^N t_j}{\sum_{j=1}^N 1}$$

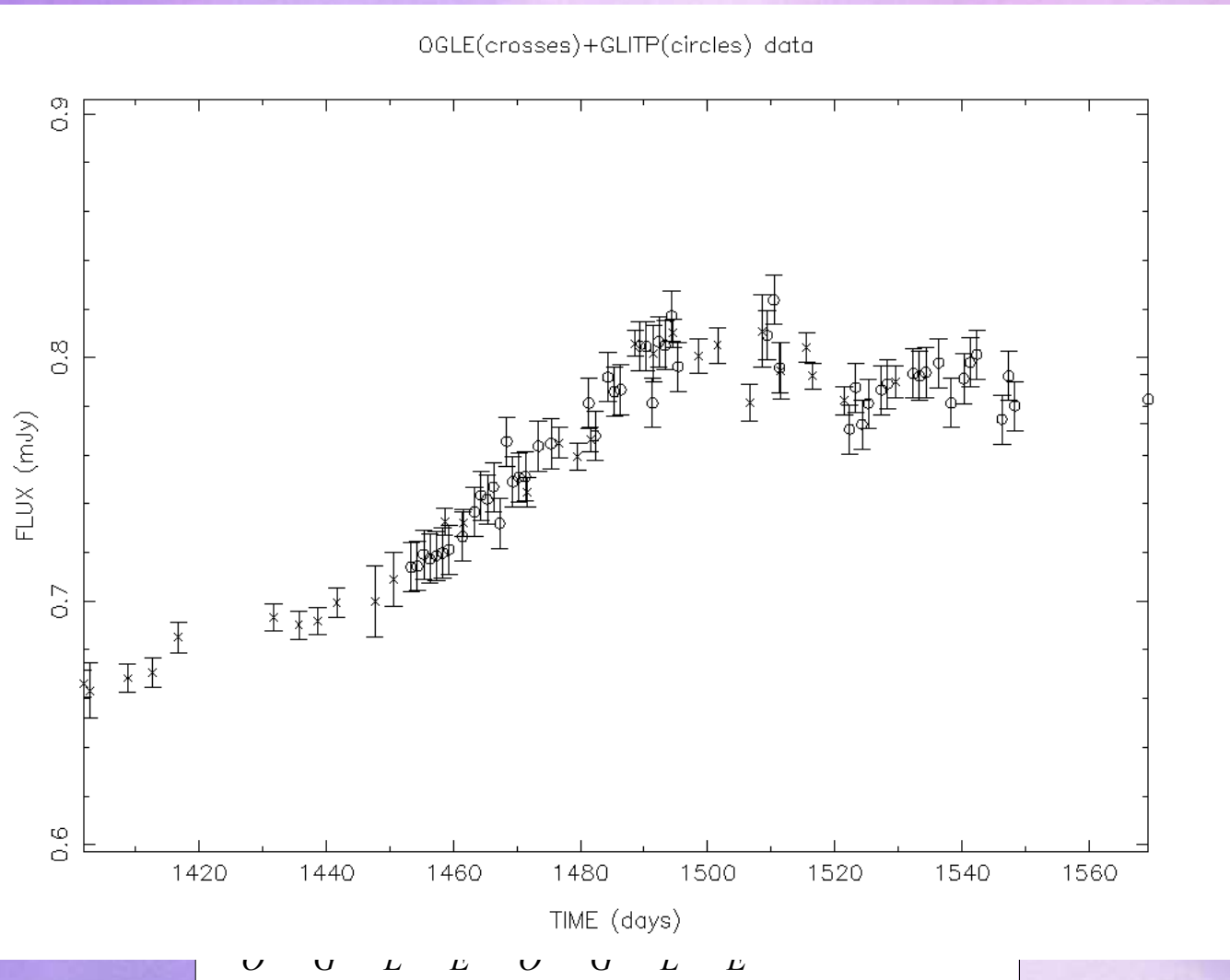


$$\frac{t_i \leq \epsilon}{t_i \leq \epsilon}$$

Mixture of data II

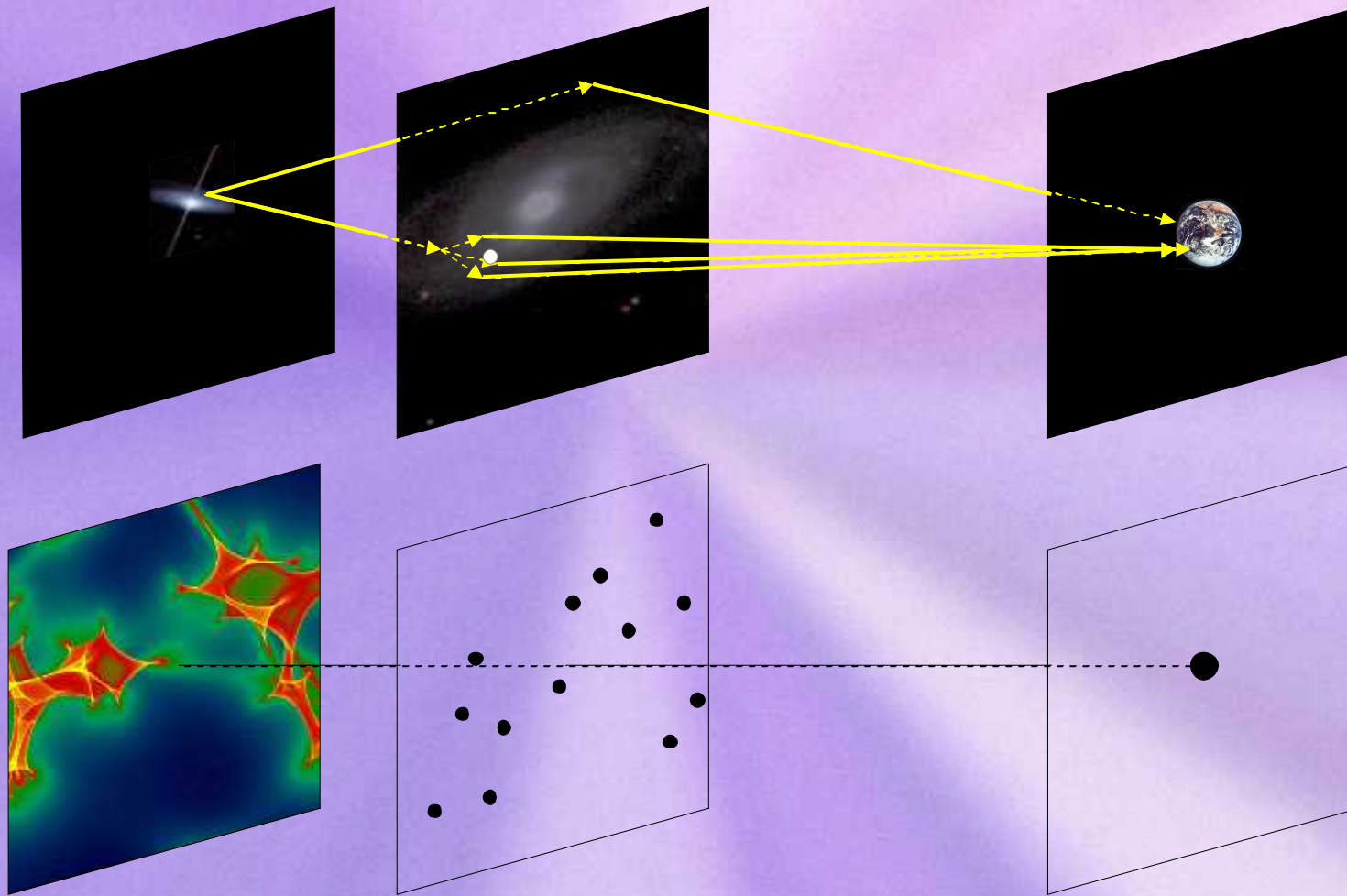
Fit b

$$\frac{\partial \chi^2}{\partial a} = 0$$

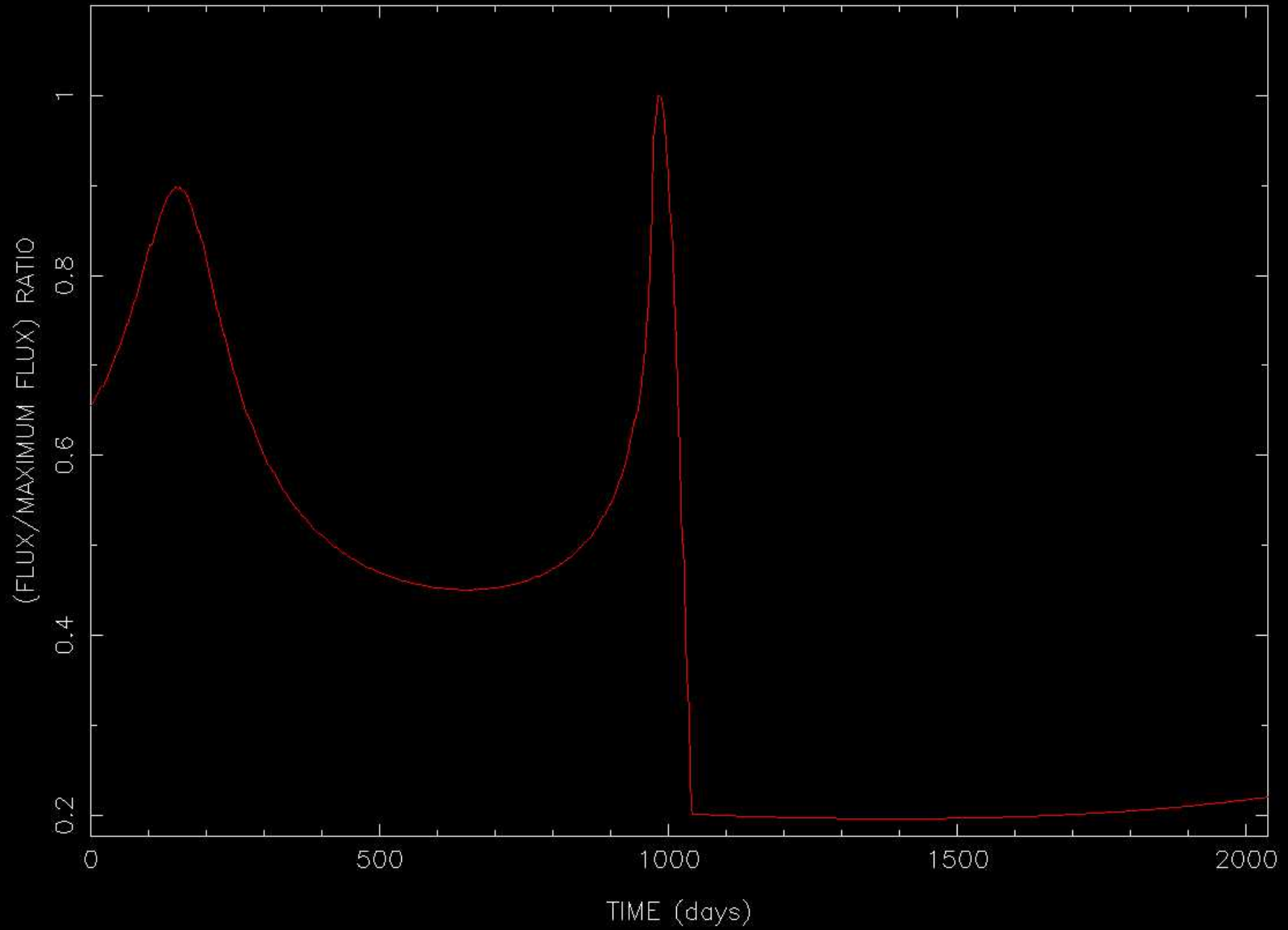


$$\sigma_{GLITP}^2$$

Microlensing modelization



SYNTHETIC LIGHTCURVE



Parameters & models I

Cosmological model

$$H_0 \equiv 66.0 \frac{Km}{Mpc \cdot s}$$

$$\Omega_m \equiv 1.0$$

$$\Omega_\Lambda \equiv 0$$

Friedman-Lemaitre's Universe

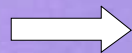


$$d_A(z_i, z_j) \equiv \frac{2c}{H_0} \times \frac{(1 - \Omega - \sqrt{1 + \Omega \cdot z_i} \cdot \sqrt{1 + \Omega \cdot z_j}) \cdot (\sqrt{1 + \Omega \cdot z_i} - \sqrt{1 + \Omega \cdot z_j})}{\Omega^2 \cdot (1 + z_i) \cdot (1 + z_j)^2}$$

$$z_o \equiv 0$$

$$z_d \equiv 0.03$$

$$z_s \equiv 1.69$$



$$D_d \equiv d_A(0, z_d) \approx 165 \text{ Mpc}$$

$$D_s \equiv d_A(0, z_s) \approx 1317 \text{ Mpc}$$

$$D_{ds} \equiv d_A(z_d, z_s) \approx 1253 \text{ Mpc}$$

Parameters & models II

Lens plane model

Mass of microlenses

$$m_1 = 0.6 \frac{M}{M_\odot}$$

$$m_2 = 0.1 \frac{M}{M_\odot}$$

$$m_3 = 0.05 \frac{M}{M_\odot}$$

Transversal velocity of microlenses

$$v_{d, \bar{r}=1} = 0.0 \frac{K}{s} n$$

$$v_{d, \bar{z}=3} = 0.0 \frac{K}{s} n$$

$$v_{d, \bar{s}=6} = 0.0 \frac{K}{s} n$$



$$v_{s, \bar{r}=7.65} = 7.65 \frac{K}{s} m$$

$$v_{s, \bar{z}=2.296} = 2.296 \frac{K}{s} n$$

$$v_{s, \bar{s}=4.592} = 4.592 \frac{K}{s} n$$

$$\frac{r}{v} = \frac{1}{1+z_s} \frac{r}{s} - \frac{1}{d_d} \frac{D_r}{D_d} \frac{1}{1+z_d} \frac{D}{D} \frac{r}{v_s}$$

Parameters & Models III

Source plane model

Geometry of the source \longrightarrow circular

$$R_p = 6 \times 10^{14} m$$

$$R_m = 2 \times 10^{15} m$$

$$R_g = 6 \times 10^{15} m$$

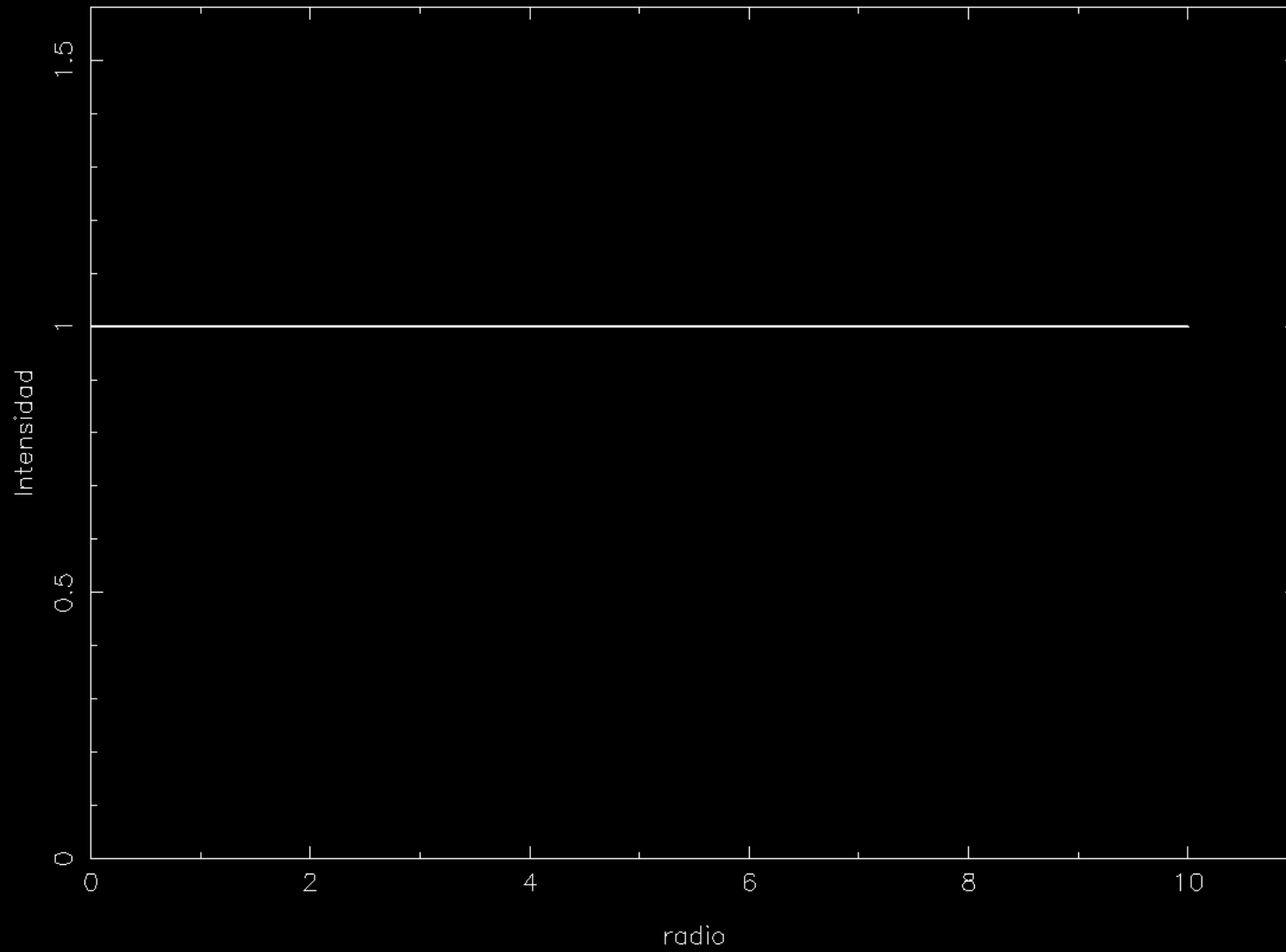
Intensity of source \longrightarrow

Uniform disk

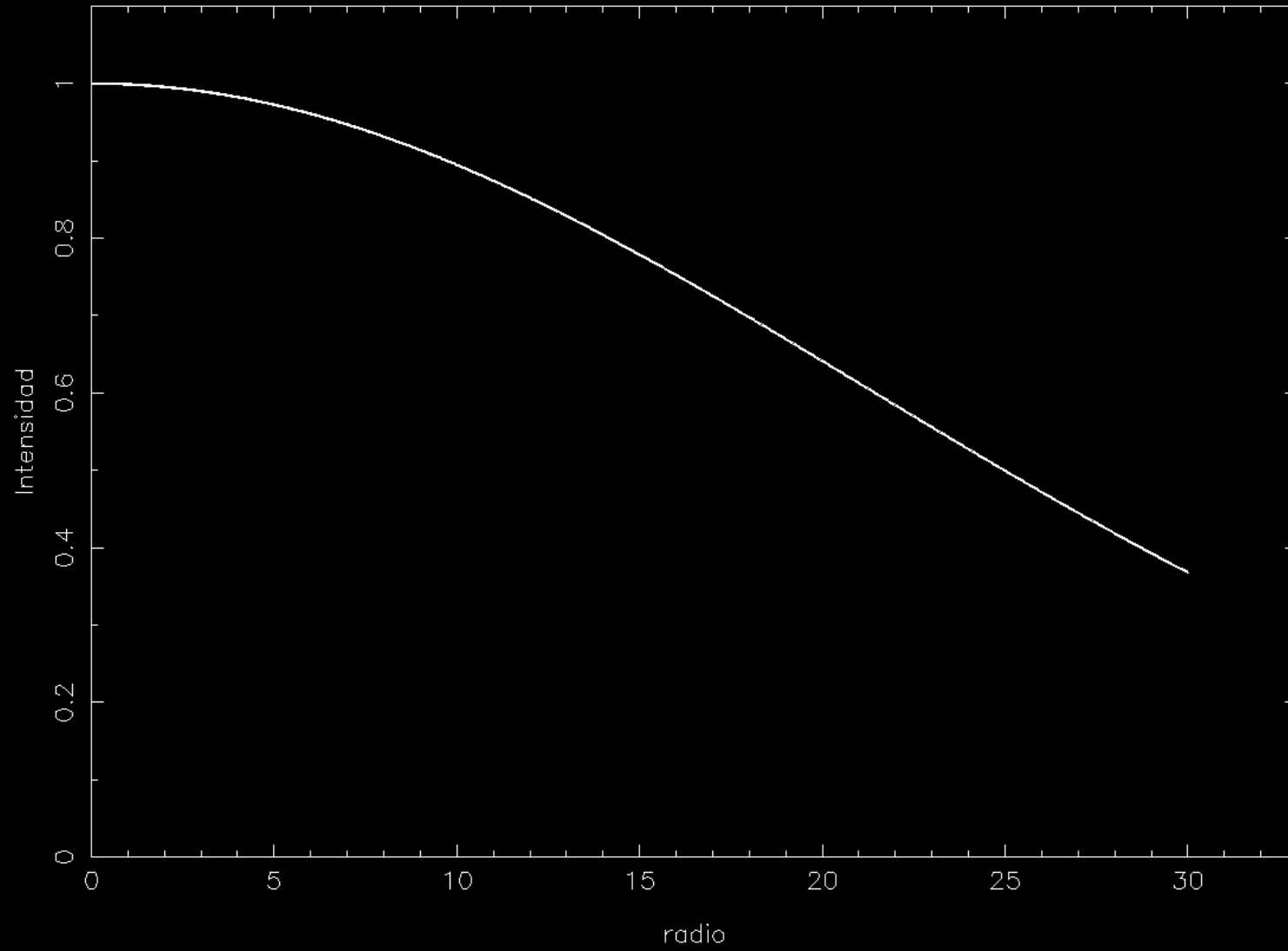
Gaussian disk

Standard accretion disk

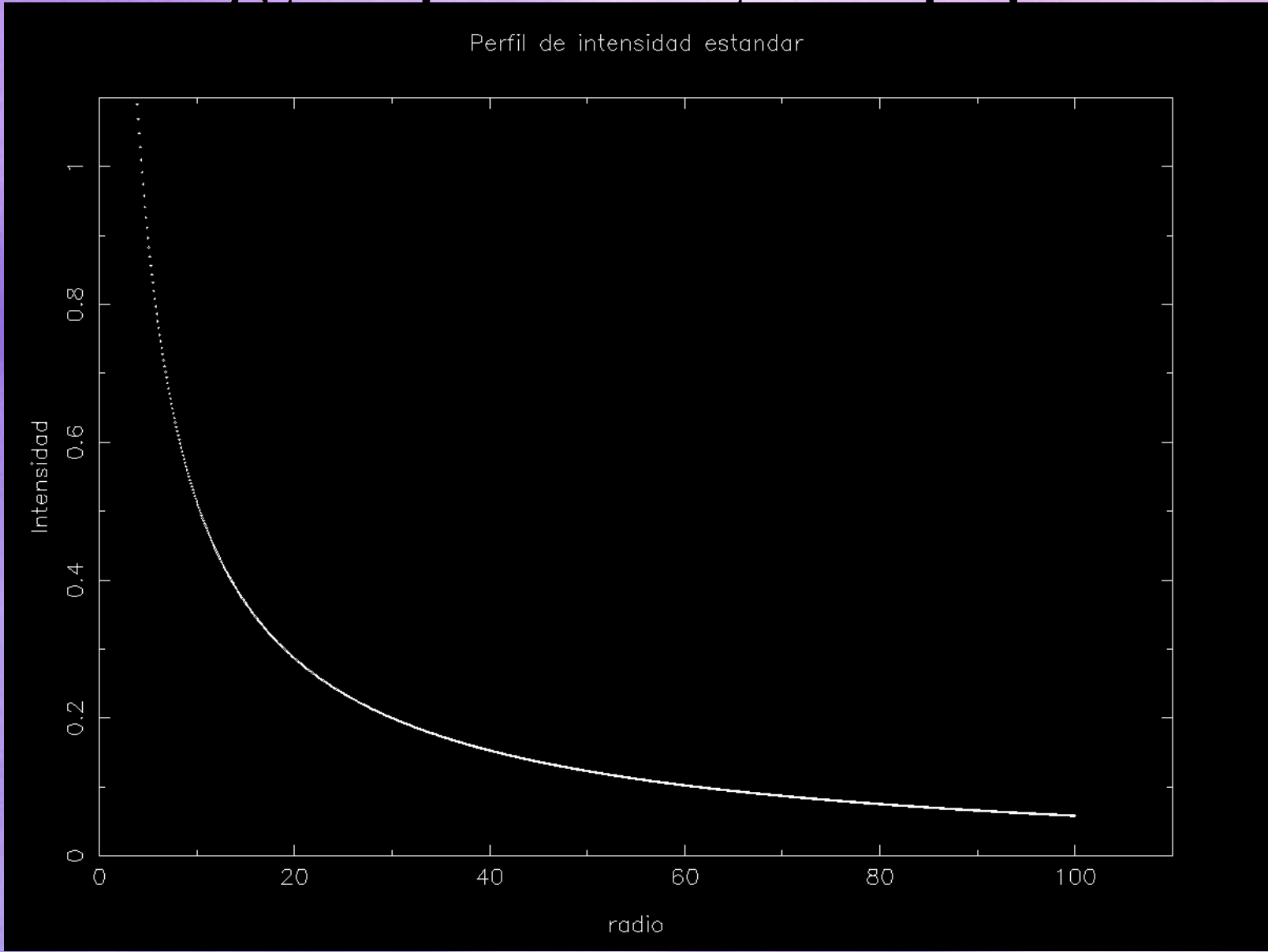
Perfil de intensidad uniforme



Perfil de intensidad gaussiano



Perfil de intensidad estandar



Observations Vs Simulations

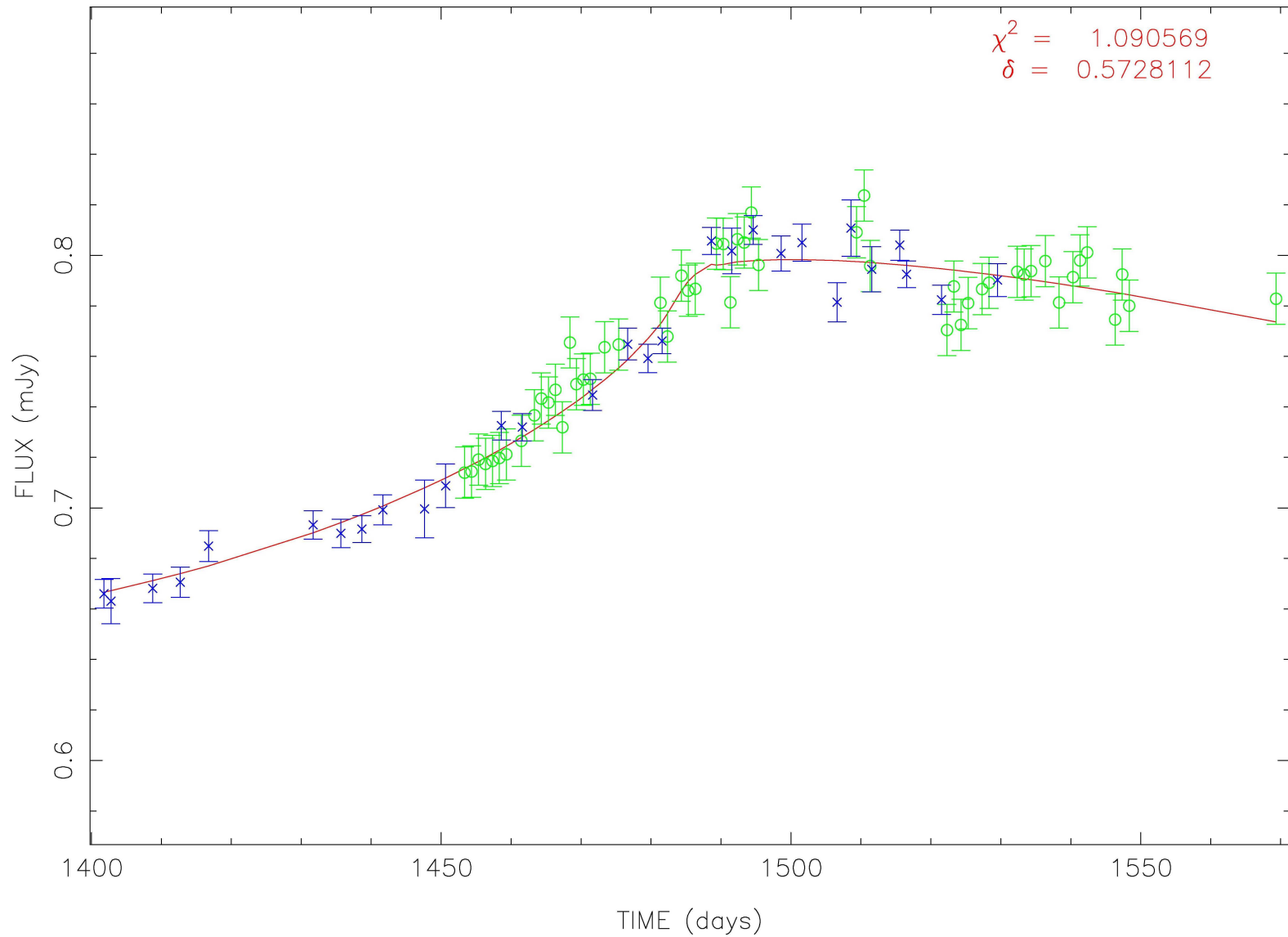
Test χ^2

$$\chi^2 = \sum_{i=1}^N \left[\frac{f_{sim}(t_i) - f_{obs}(t_i)}{\sigma_{obs}(t_i)} \right]^2$$

Test δ

$$\sigma = \sqrt{2 \cdot v} \quad \longrightarrow \quad \delta = \frac{|\chi^2 - v|}{\sqrt{2 \cdot v}} \leq 1$$

SYNTHETIC LIGHTCURVE NUMBER 1 FOR 600010stp02



Results I: Best parameters

Parametrization	Trayectories with $\delta < 1$	% of trayectories with $\delta < 1$	$\langle \hat{\chi}^2 \rangle$	$\sigma_{\hat{\chi}^2}$	$\hat{\chi}_{\min}^2$
300010sts02	3	6 %	1.145	0.002	1.141
300060sts01	1	2 %	1.147	0.000	1.147
300060sts02	3	6 %	1.110	0.010	1.083
600005sts03	14	26 %	1.109	0.008	1.063
600010sts02	27	50 %	1.117	0.003	1.091
600060stm01	5	9 %	1.143	0.006	1.127
600060sts02	1	2 %	1.107	0.000	1.107

Results II: Best source model

SOURCE MODEL (intensity+size)	Trajectories with $\delta < 1$	% of trajectories with $\delta < 1$
Standar accretion disk small	49	91 %
Standar accretion disk medium	5	9 %

Results III: Best microlenses model

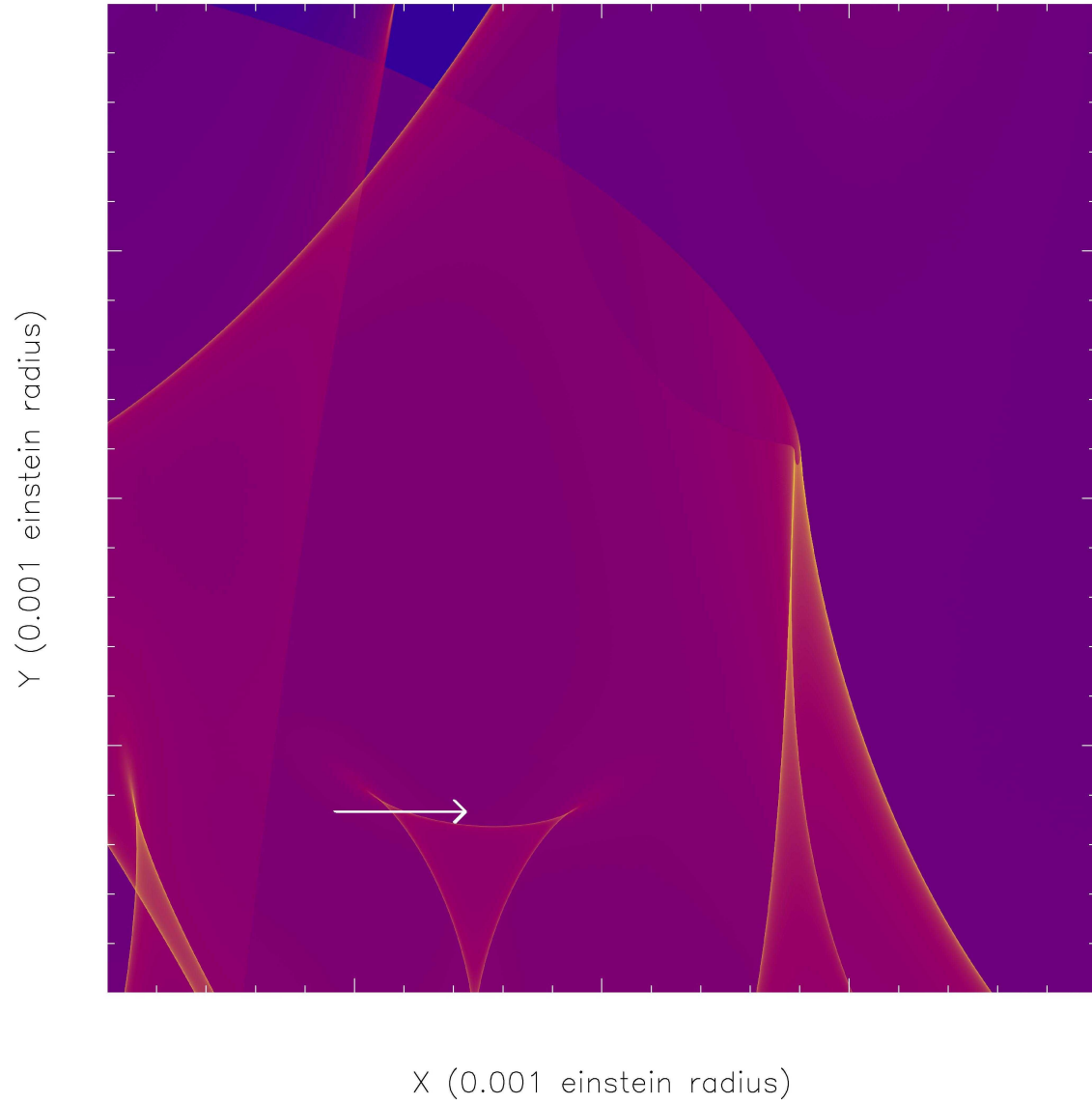
MICROLENS MODEL (velocity+mass)	Trayectories with $\delta < 1$	% of trayectories with $\delta < 1$
$v_d = 300$ $m = 0.10$	3	6 %
$v_d = 300$ $m = 0.60$	4	7 %
$v_d = 600$ $m = 0.05$	14	26 %
$v_d = 600$ $m = 0.10$	27	50 %
$v_d = 600$ $m = 0.60$	6	11 %

Results IV: Caustic crossing?

Parametrization	Trajectories with $\delta < 1$	Number of caustic crossing events	% of caustic crossing events for that parametrization
300010sts02	3	3	100 %
300060sts01	1	1	100 %
300060sts02	3	3	100 %
600005sts03	14	0	0 %
600010sts02	27	27	100 %
600060stm01	5	5	100 %
600060sts02	1	1	100 %

$$\frac{\text{non caustic crossing trajectories } 14}{\text{trajectories } 54} = \frac{14}{54} \approx 25.93\%$$

Magnification pattern for QSO 2237+0305A (2x2 einstein radius)



Future steps

New observational data

New magnification patterns

New parametrizations