

# Lens Galaxy Environments

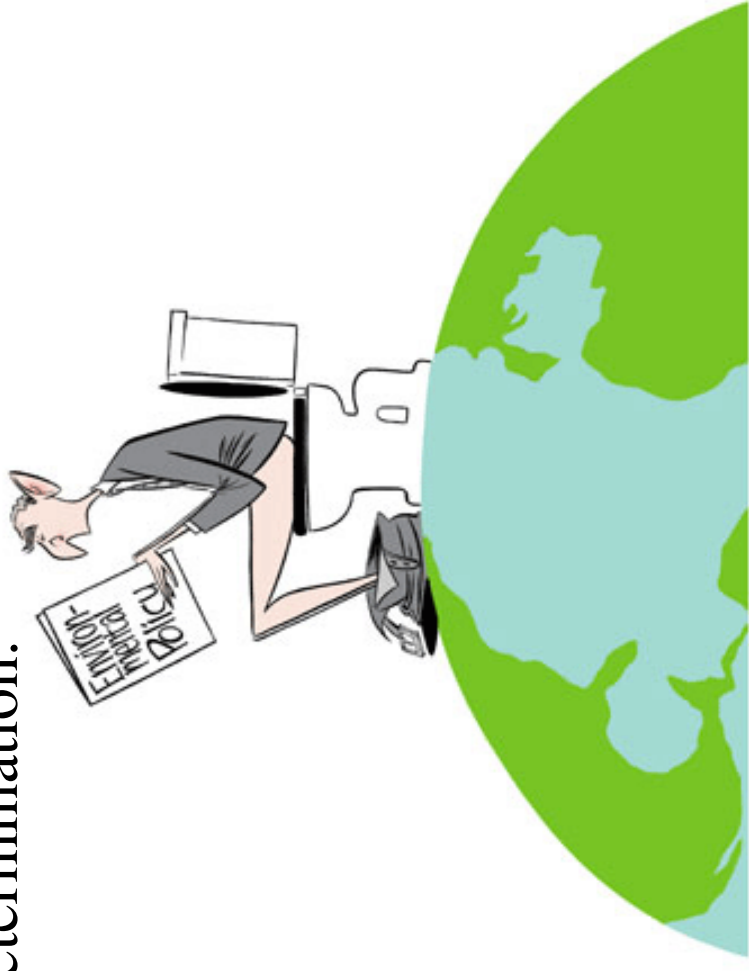
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astro-ph/0409483

1. Who cares?
2. What to do
3. Results
4. **Problems!**
5. The future



# Does environment matter?

- Yes! Environment can generate shear at lenses, which affects image morphology, multiplicity...
- Also, projected mass at lenses leads to mass-sheet degeneracy, impeding  $H_0$  determination.



# The need for external shear

Single-galaxy models fail. PG1115+080:

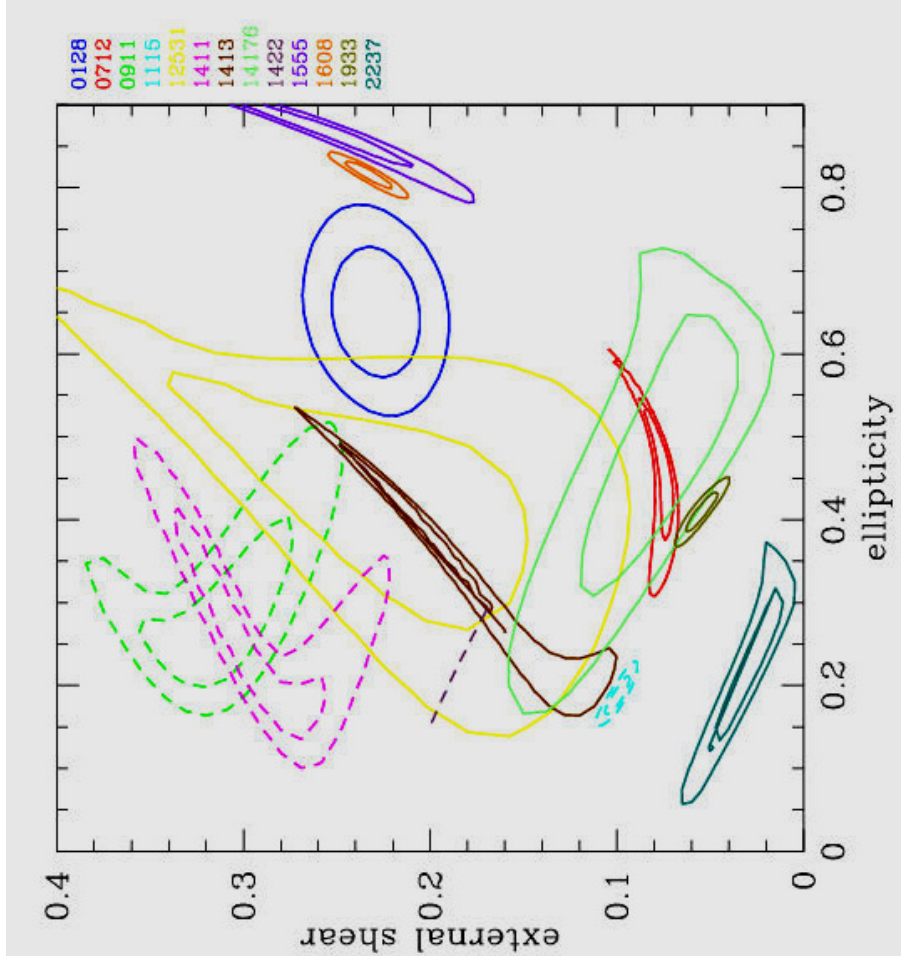
- data:  $\sigma_x = 2$  mas
- models:  $\delta x \sim 40$  mas

Changing the model doesn't help.

Need an **external tidal shear**.

- models:  $\delta x \sim 0.2$  mas

Quads:



*(from Chuck Keeton)*

# Input from theory

In CDM model, halo mass and environment are closely related : more massive halos cluster more strongly, and we know quantitatively how halo clustering depends upon mass (e.g. Mo & White, Seljak & Warren 2004)

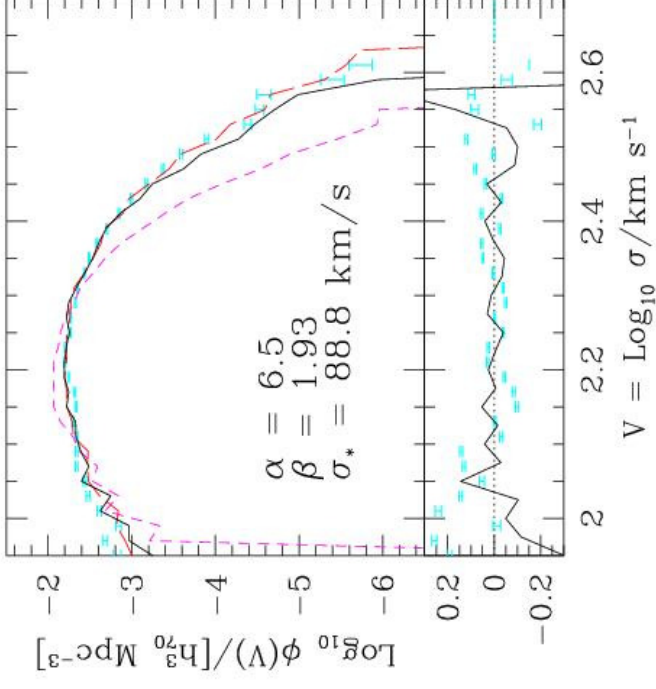
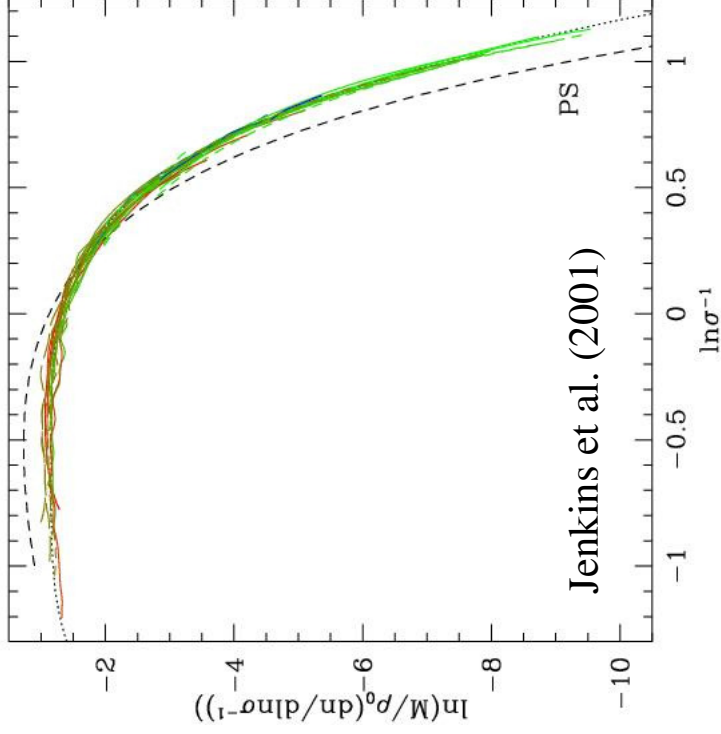
So assessing importance of lens environments means determining: **where (in which halos) do lenses live?**

Fortunately, we can begin to answer this question with recent results from SDSS

1. number counts (Sheth et al. 2003)
2. tangential shear profiles (Sheldon et al. 2004)

# Number counts of massive ellipticals

Most lenses are massive ellipticals, and [Sheth et al. \(2003\)](#) have measured their number density in SDSS as a function of velocity dispersion.



Since we know the theoretical mass function of DM halos, this constrains the halo occupation distribution of massive elliptical galaxies.

# Tangential shear profiles

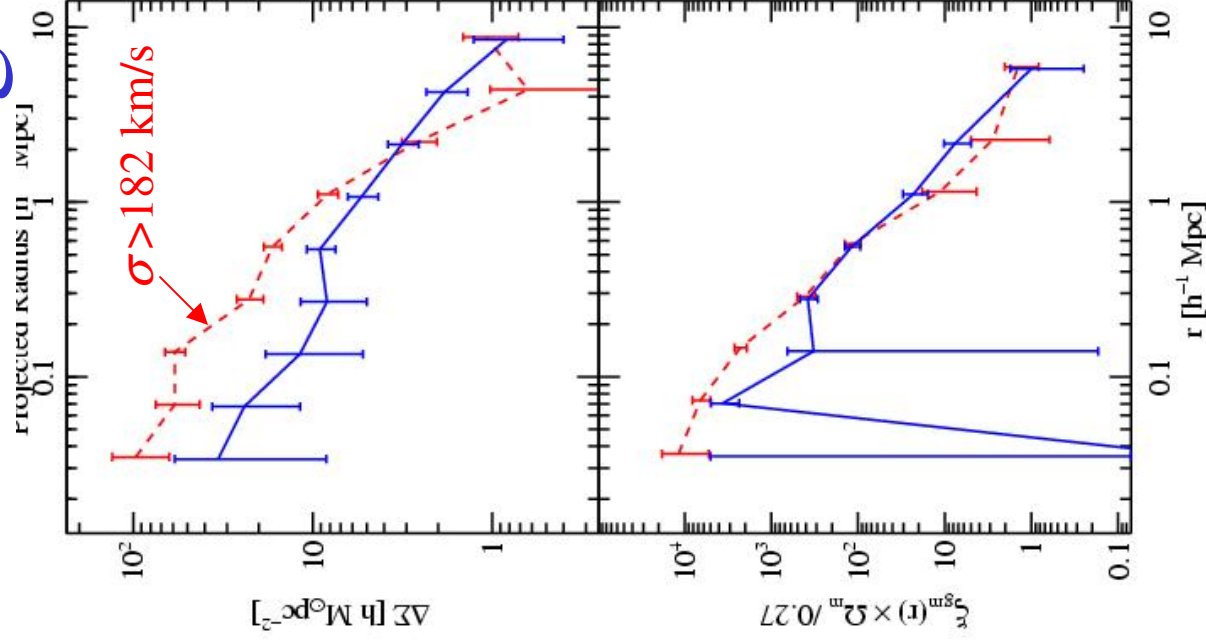
Sheldon et al. (2004) have measured the average tangential shear profile around massive SDSS elliptical galaxies. This constrains the galaxy-mass correlation function and power spectrum

$$\langle \gamma_{\text{tan}} \rangle(\theta) = \int \frac{l dl}{2\pi} C_l^{gK} J_2(l\theta)$$

$$C_l^{gK} \sim \int dz P_{gm} \left( k = l / r(z) \right)$$

In the halo model,  $P_{gm}$  contains several pieces

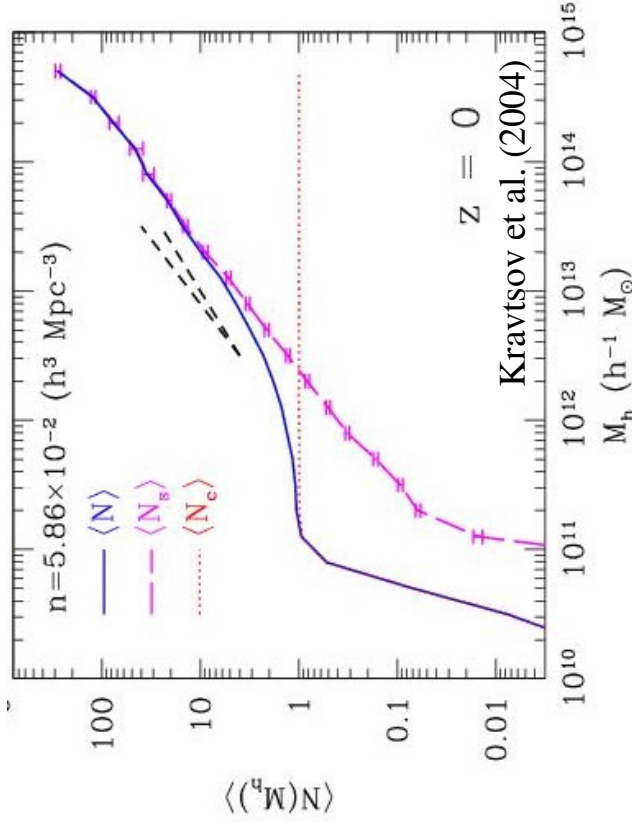
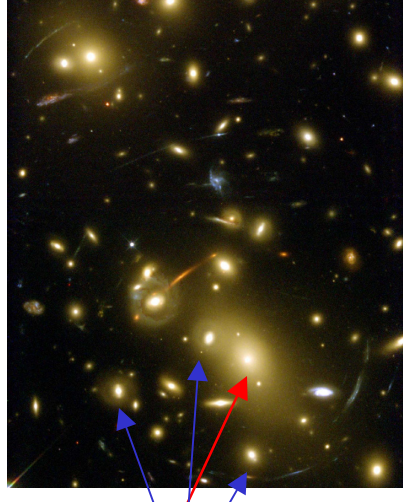
1. density profiles of galaxies' own halos
2. profiles of parent halos for satellites
3. nearby correlated halos (2-halo term)



# Halo occupation distribution

To fit SDSS data, we need a model for the HOD. Simulations (N-body, SPH, semi-analytic) find that the HOD has two distinct pieces:

1. Central galaxies sitting at potential minimum (e.g. field galaxies, cluster cD galaxies)
2. Satellites: (other galaxies in groups or clusters)



Each piece has simple behavior:

1. Central galaxies, either present or not, with
2. Satellites: Poisson random # with mean

$$\langle N_{\text{cen}} \rangle(M) = \Theta(M - M_{th})$$

$$\langle N_{\text{sat}} \rangle(M) = \left( \frac{M}{A \cdot M_{th}} \right)^m$$

so total number is  $\langle N \rangle = \langle N_{\text{cen}} \rangle + \langle N_{\text{sat}} \rangle$

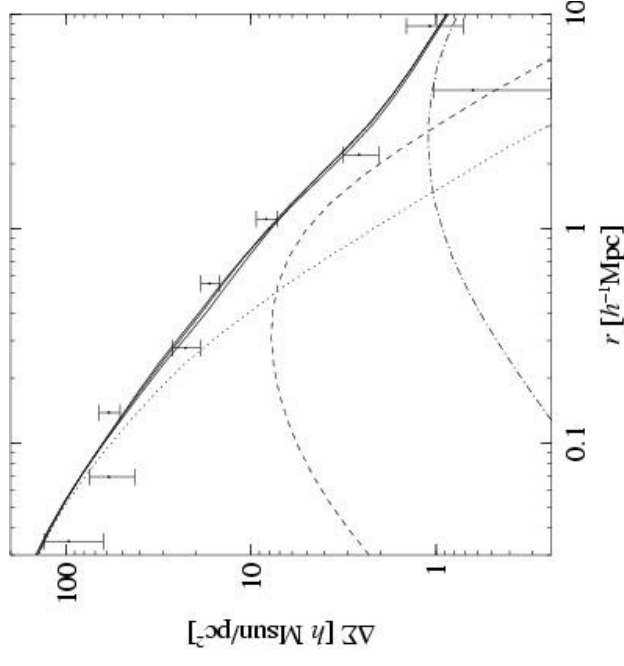
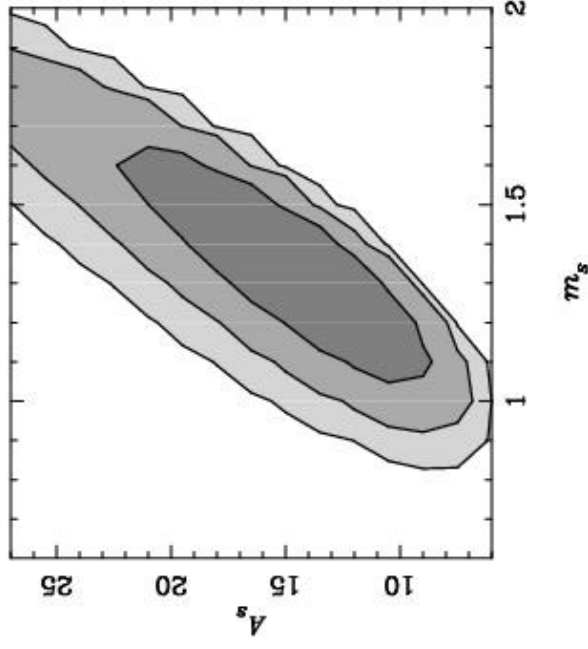


# Fit to SDSS data

Our HOD has 3 free parameters : (note halo parameters are not free!)

1.  $M_{th}$ : lowest mass halo which can host a lens galaxy
2.  $A$ : controls the fraction of lenses that are satellites
3.  $m$ : controls whether satellite lenses are placed mostly in low mass halos (e.g. poor groups) or high mass halos (e.g. clusters)

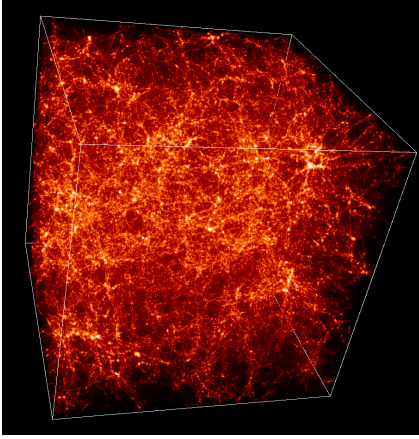
Found  $M_{th} \sim 10^{12.5} M_{sun}$  tightly constrained, but  $A$  and  $m$  are degenerate



Can improve constraints with measurements of multiplicity function from SDSS or DEEP2



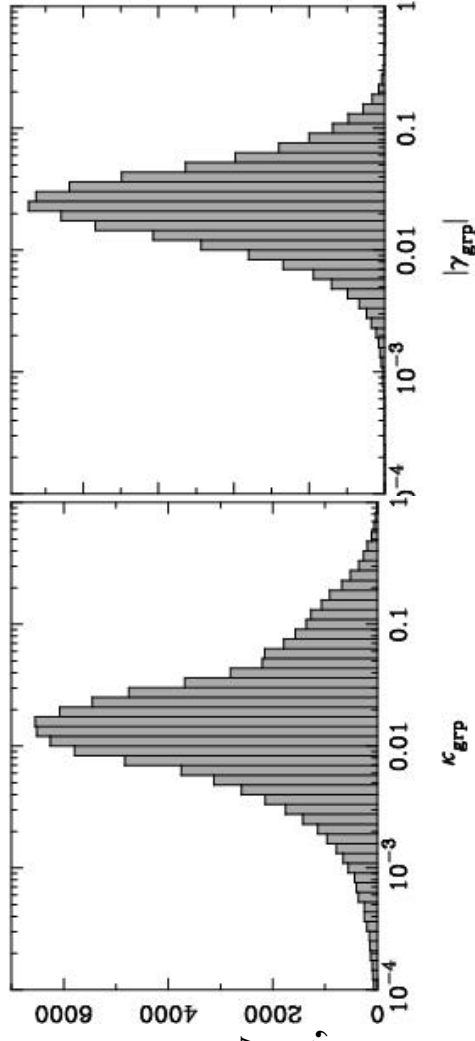
# N-body simulation



Next we used this HOD to populate a  $256^3$  particle  $\Lambda$ CDM simulation with WMAP parameters in  $256 h^{-1}\text{Mpc}$  box. We ran FOF to find halos, and populated the halos with lens galaxies using our best-fitting HOD. Then we projected the box and computed convergence and shear at the galaxy positions.

## Results:

1. typical  $\kappa_{\text{env}} \approx |\gamma_{\text{env}}| \approx 0.03$
2. stronger events occur more rarely  
e.g.  $\kappa > 0.1$  occurs 6% of the time,  
 $|\gamma| > 0.1$  occurs 3% of the time.

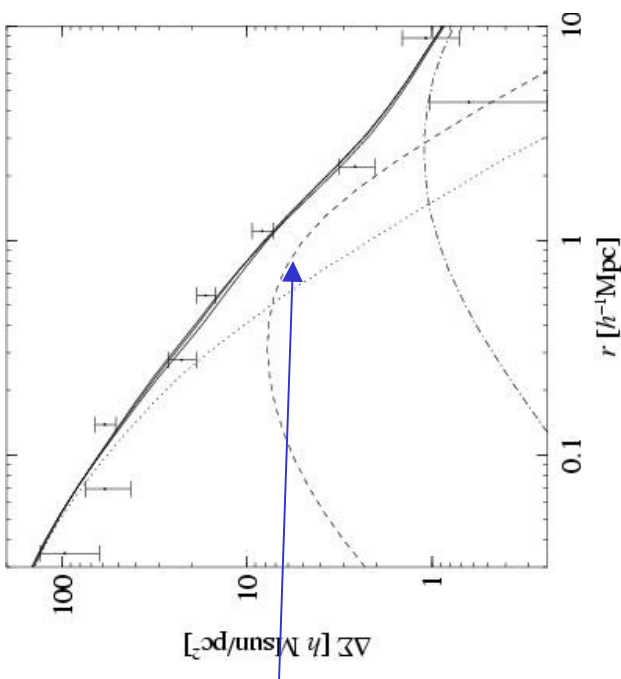


So environment shouldn't significantly bias  $H_0$ . But note that there remains one puzzling **discrepancy**: our shear values are far below the  $\gamma \sim 15\%$  external shear found in models of strong lenses!

# Too much shear?

There was a broad degenerate region in parameter space  
– are there models which match strong lensing results?

No – the group contribution to  $\gamma_{\text{tan}}$  is dominant on Mpc scales, so we can't increase it by factor of  $\sim 5$  without grossly violating g-g lensing constraints.

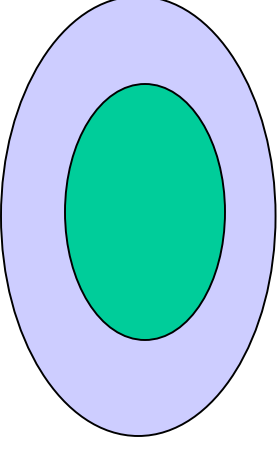


Are there other sources of shear to explain strong lensing?

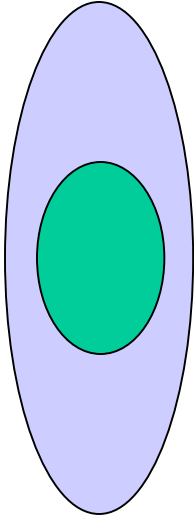
- **projected LSS in line-of-sight?** Doesn't work because cosmic shear measurements limit this to  $\gamma \sim 1-2\%$ .
- **lens halos?** External shear in strong lenses could originate in the lenses' own halos (Keeton et al. 1997), but this also has difficulties...

# How to make shear

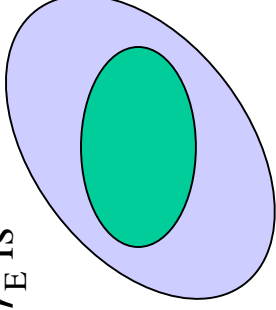
**Newton:** if density is stratified on concentric ellipses of constant ellipticity, then material on ellipses exterior to a point have no effect at that point.



To produce shear, the halo material must either have a different ellipticity, or be twisted relative to galaxy. For isothermal profile with Einstein radius  $r_E$ , if we distort shape at radius  $r_0$ , then induced shear at  $r_E$  is



$$\Delta\gamma \sim \frac{r_E}{r_0} \frac{\Delta\epsilon}{2\pi}$$



$$\Delta\gamma \sim \frac{r_E}{r_0} \frac{\epsilon}{\pi} \sin^2 \Delta\theta$$

**Problem:** Hoekstra et al. (2004) find that galaxies align with their extended halos, with

$$\langle \epsilon_{\text{halo}} \rangle \geq 0.7 \langle \epsilon_{\text{gal}} \rangle \Rightarrow \Delta\gamma \leq 0.3 \frac{\epsilon}{2\pi} \frac{r_E}{r_0}$$

so for lens halos to produce the excess shear, there must be drastic changes in density structure at  $r \sim r_E$  (another way of saying that the model has problems).

# Conclusions

1. Current SDSS data indicate that environment should be unimportant for typical strong lensing systems; typically  $\sim 3\%$  errors in  $H_0$ .
2. However there may be a discrepancy between g-g lensing, which indicates  $\sim 3\%$  shear at lens galaxies, and strong lensing, which requires  $\sim 15\%$  shear.
3. There appear to be no good alternative candidates for the source of the discrepant shear; perhaps massive substructure in halo?
4. Upcoming data on multiplicity function for groups & clusters should help refine the HOD massive elliptical galaxies.