

Spectral analysis of quasar microlensing

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ANALYSIS METHODS

High Magnification Events

Statistical Methods

One-Point

Two-Points

mean,
dispersion

probability
distribution

autocorrelation
function

power
spectrum

Autocorrelation function and power spectrum

$$p(\Delta\mathbf{r}) = \langle f(\mathbf{r})f(\mathbf{r} + \Delta\mathbf{r}) \rangle \quad \text{autocorrelation function}$$

$$P(\mathbf{k}) = \left\langle \left| \int f(\mathbf{r}) \exp(-i2\pi\mathbf{k}\mathbf{r}) d\mathbf{r} \right|^2 \right\rangle \quad \text{power spectrum}$$

$$P(\mathbf{k}) = \int p(\Delta\mathbf{r}) \exp(-i2\pi\mathbf{k}\Delta\mathbf{r}) d\Delta\mathbf{r} \quad \text{Wiener-Khinchin theorem}$$

Coordinate smoothing

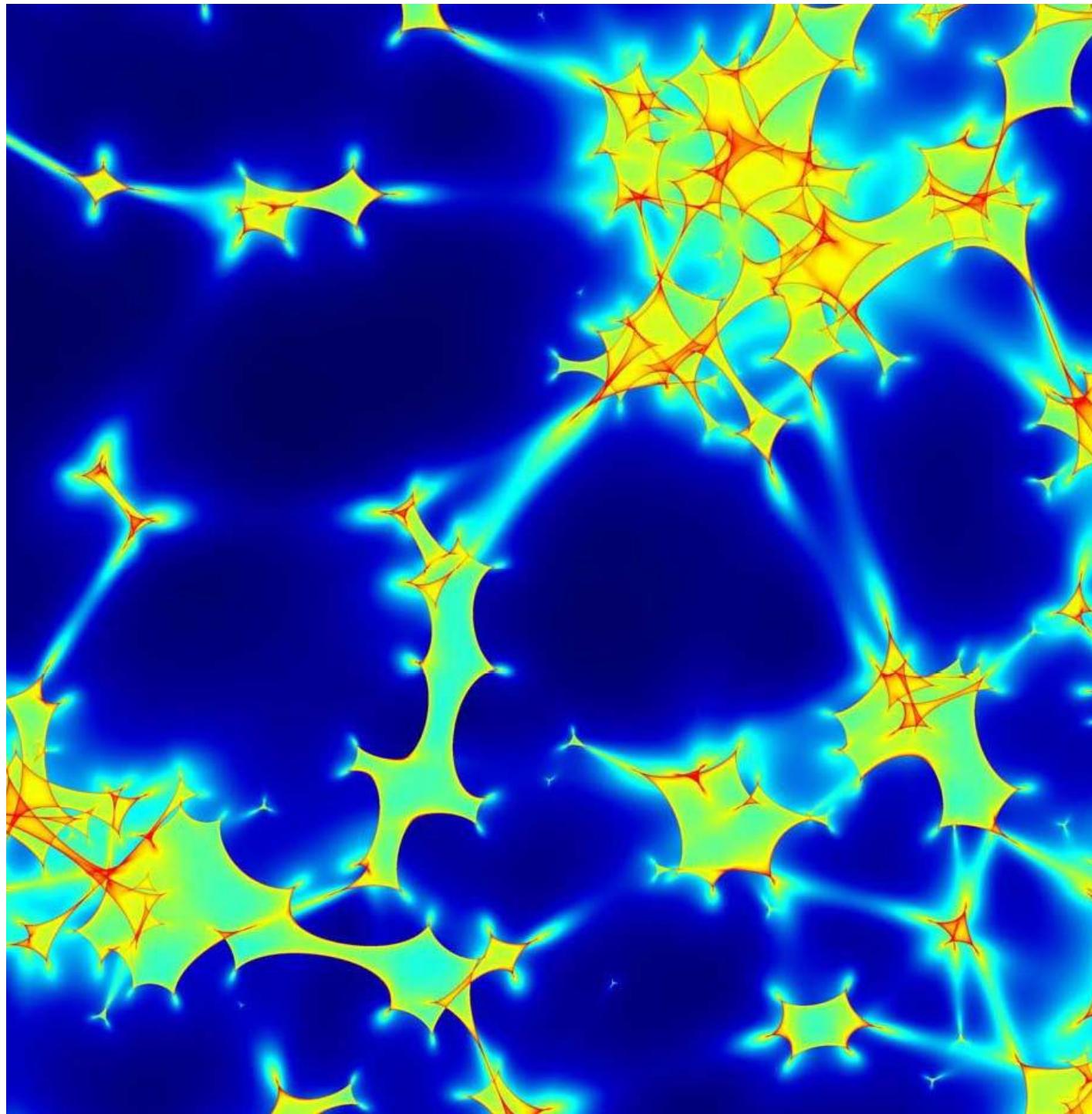
$$\int f(\mathbf{r}) h(\rho - \mathbf{r}) d\mathbf{r}$$

$$\int p(\Delta\mathbf{r}) h(\Delta\rho - \Delta\mathbf{r}) d\Delta\mathbf{r}$$

Frequency weighting

$$F(\mathbf{k})H(\mathbf{k})$$

$$P(\mathbf{k})H(\mathbf{k})$$

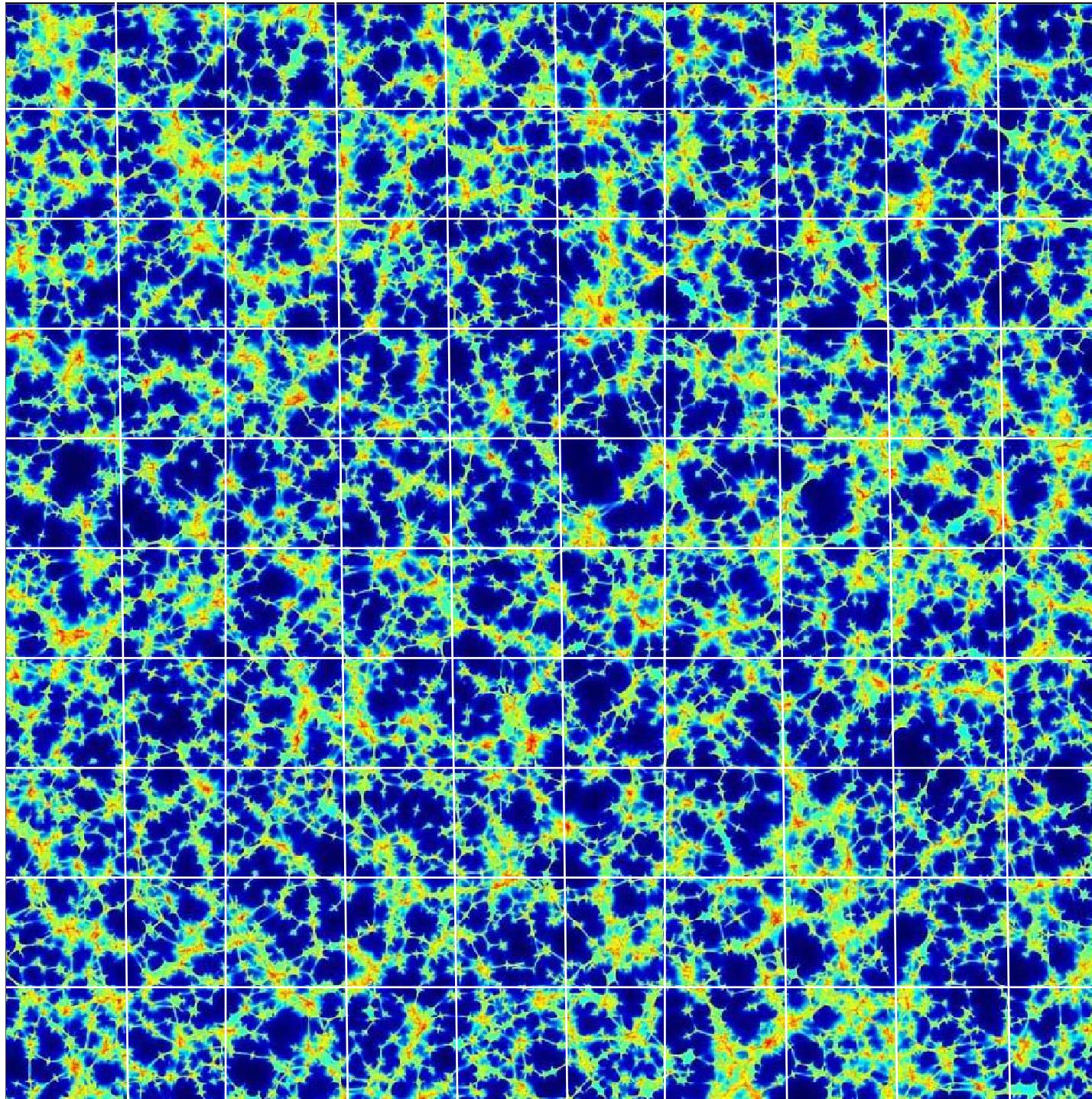


Magnification
pattern

$$k = 0.4$$

$$\gamma = 0$$

$$L = 20 R_e$$

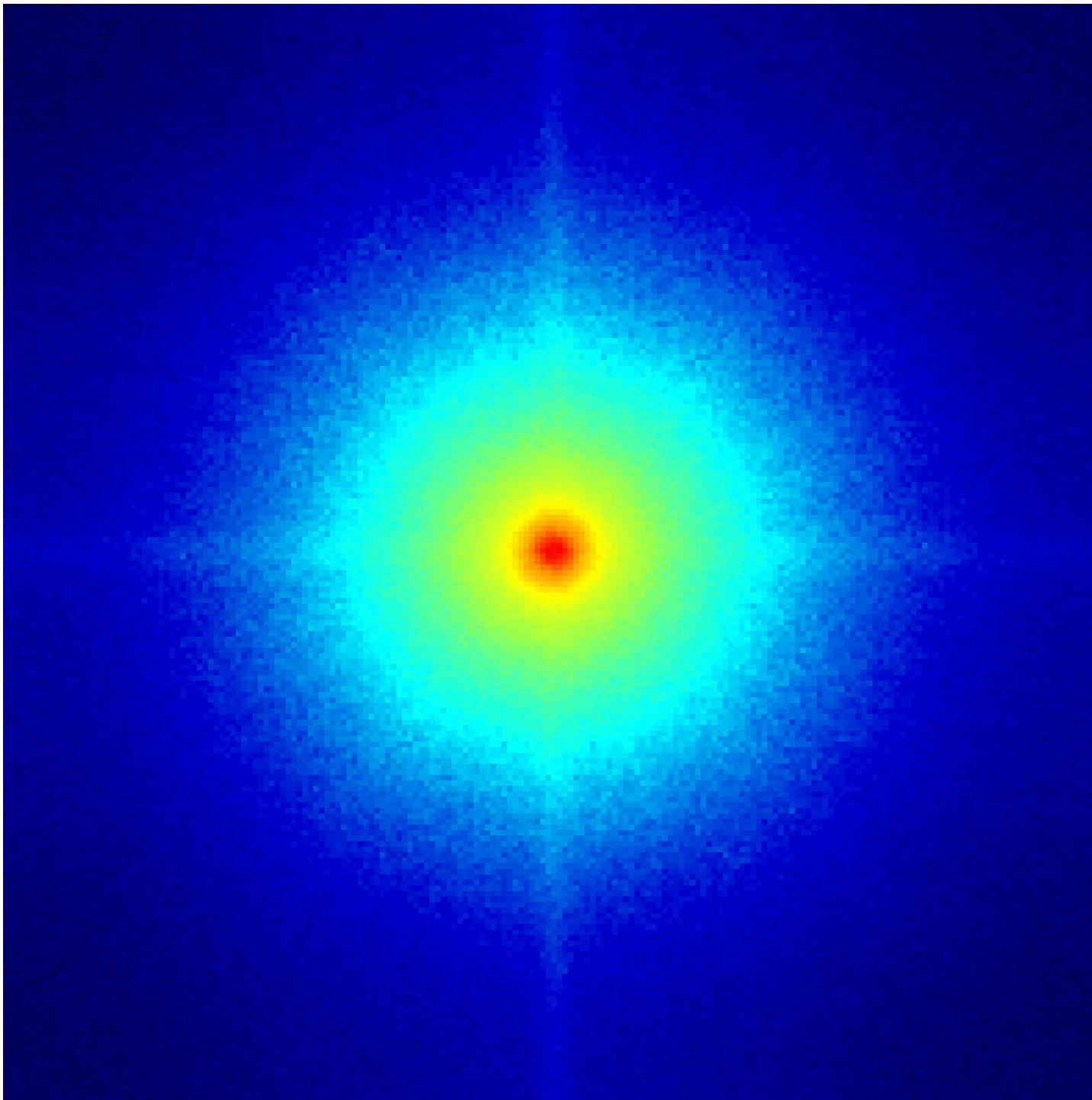


Magnification
pattern

$$k = 0.4$$

$$\gamma = 0$$

$$L = 200 R_e$$



Spectrum

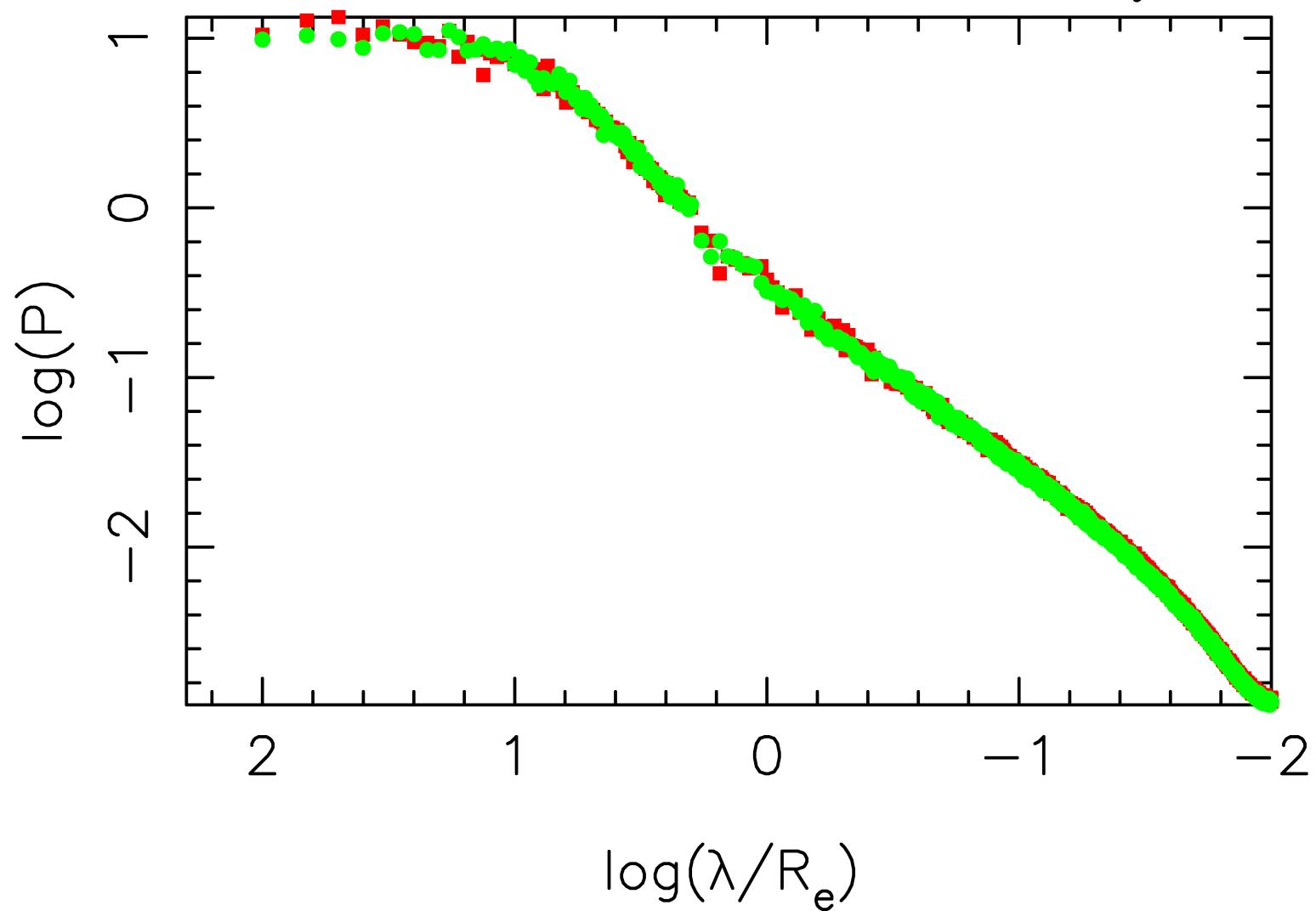
$$k = 0.4$$

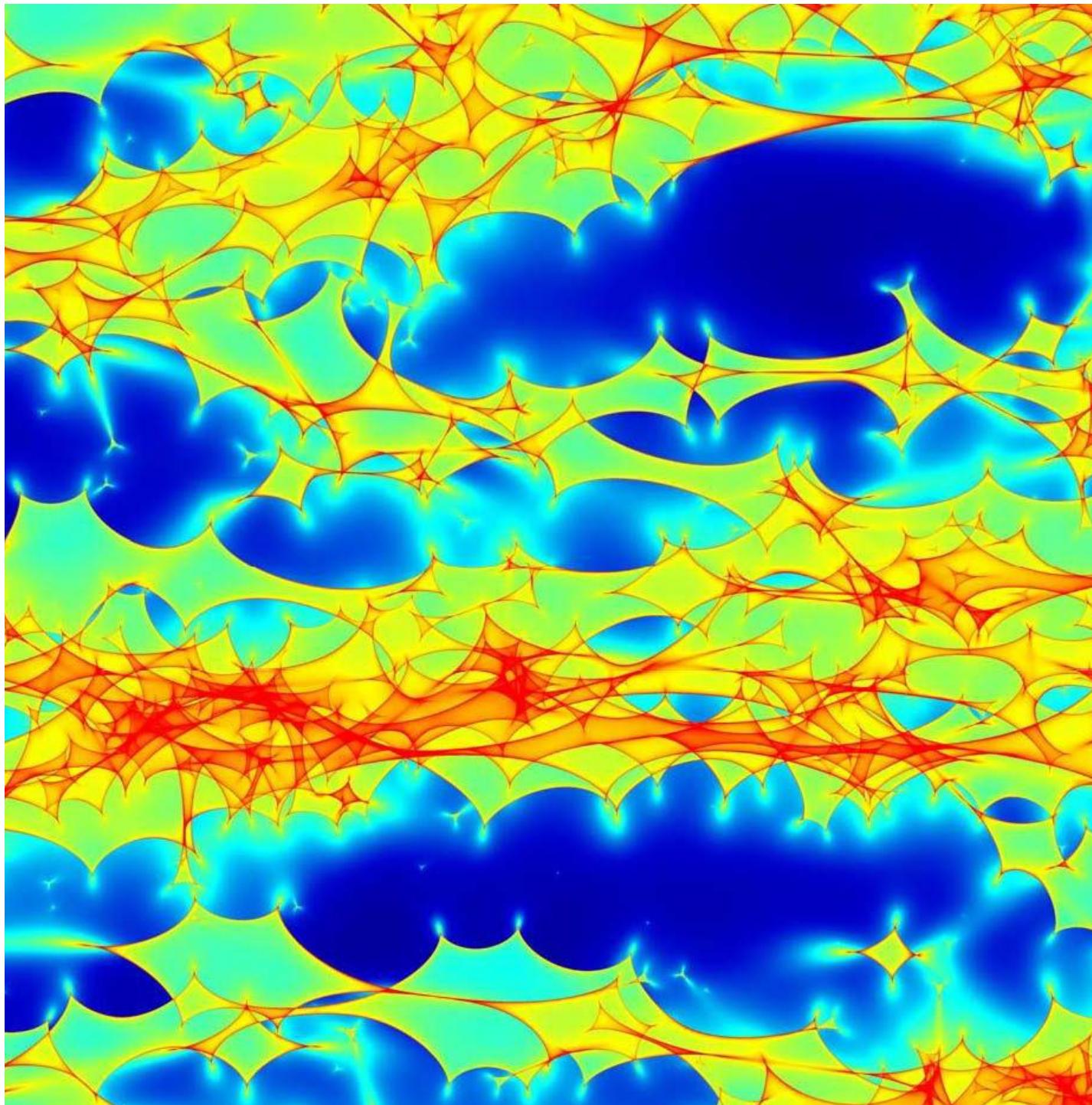
$$\gamma = 0$$

$$L = 20 R_e$$

$$P_x(k_x) = \int P(k_x, k_y) dk_y$$
$$P_y(k_y) = \int P(k_x, k_y) dk_x$$

Spectral projections $k = 0.4, \gamma = 0$



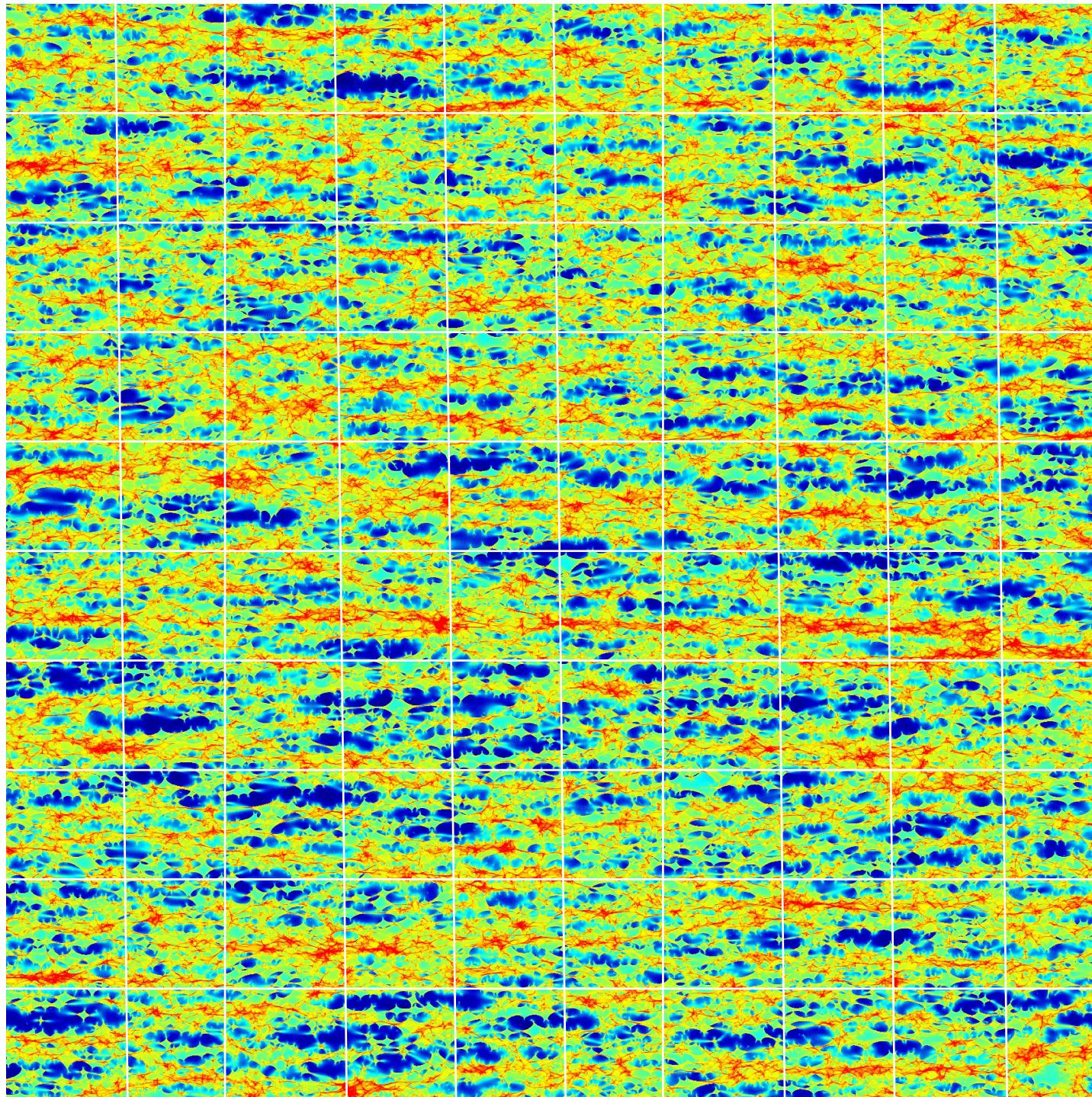


Magnification
pattern

$$k = 0.4$$

$$\gamma = 0.4$$

$$L = 20 R_e$$

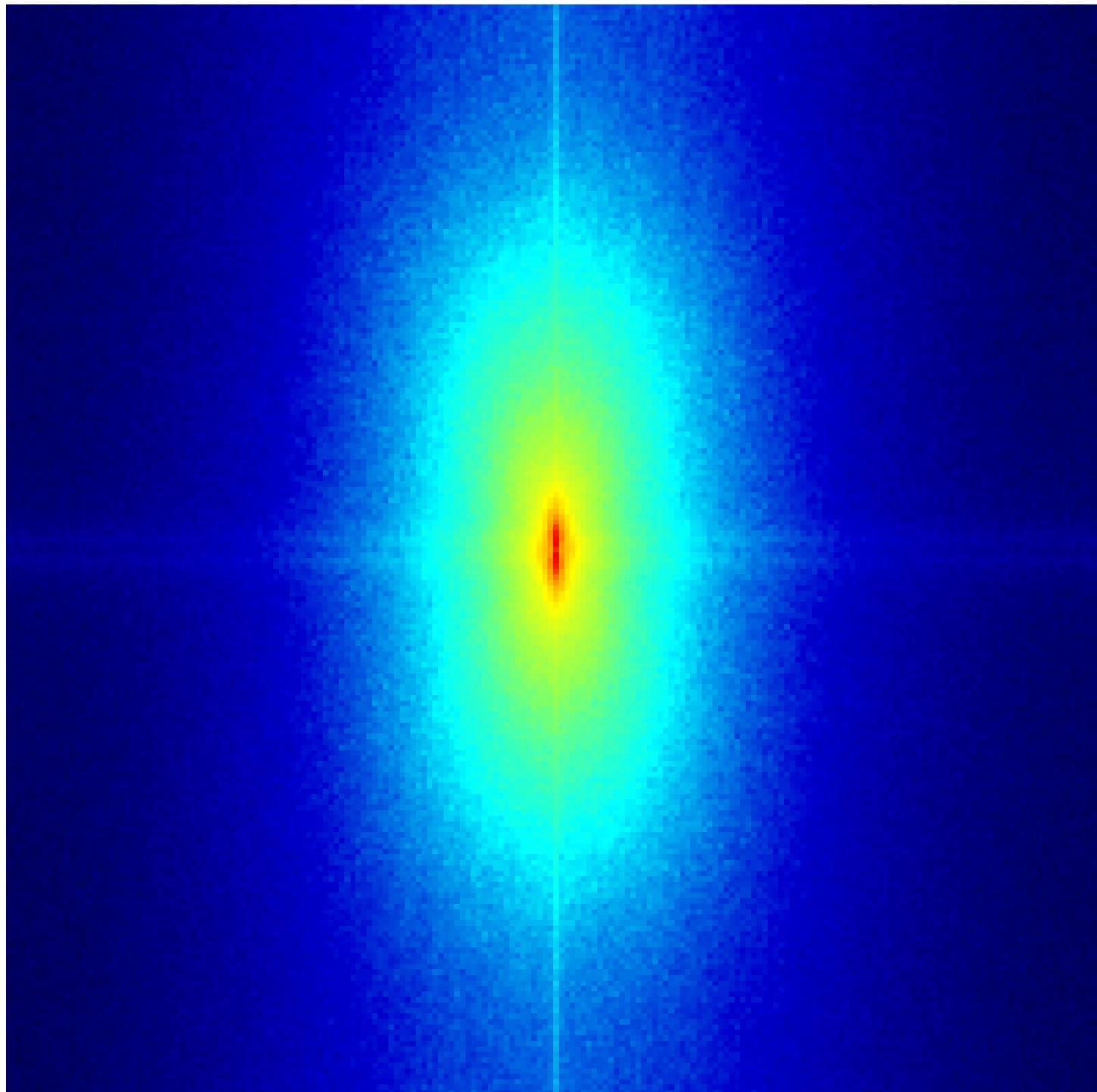


Magnification
pattern

$$k = 0.4$$

$$\gamma = 0.4$$

$$L = 200 R_e$$



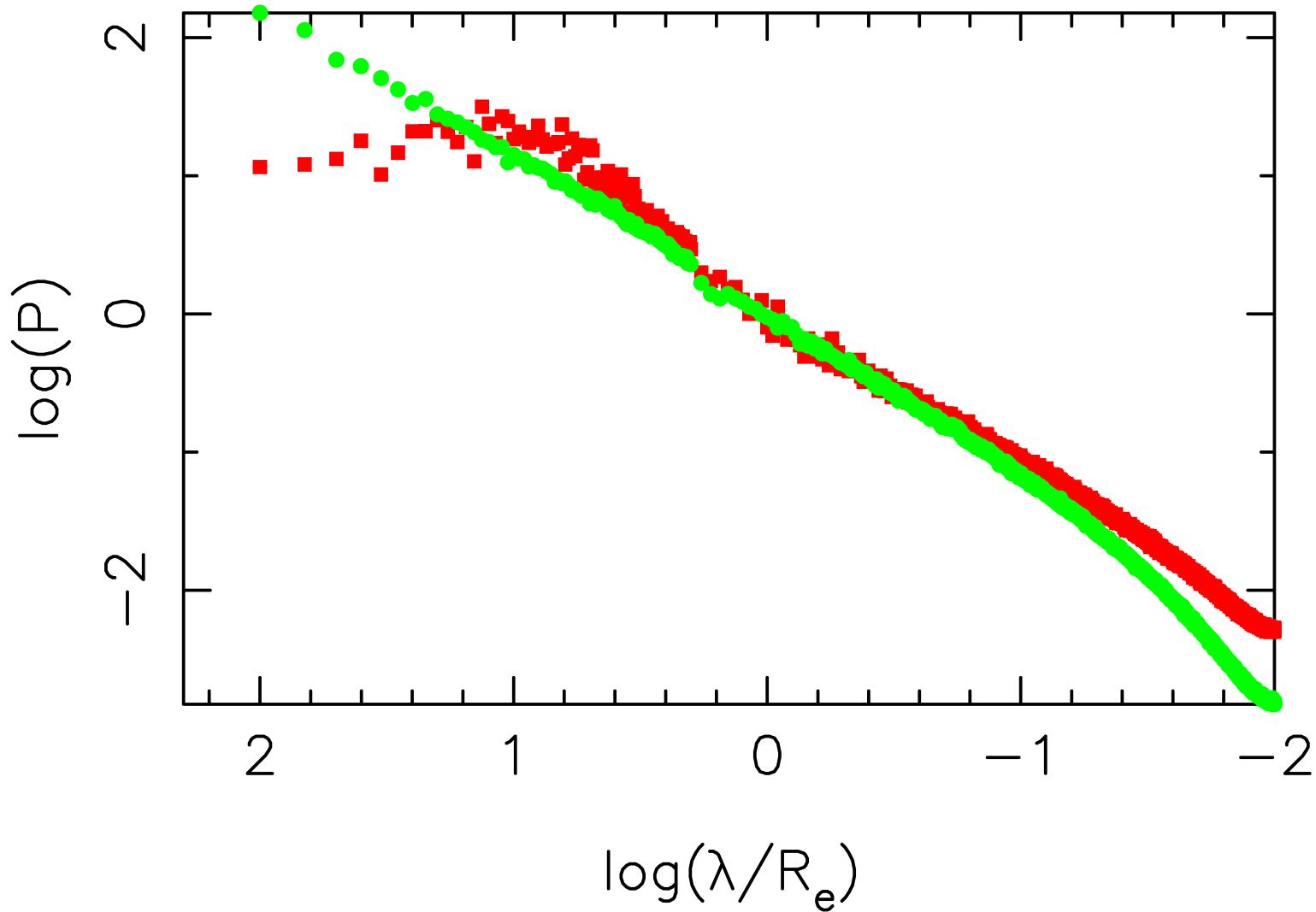
Spectrum

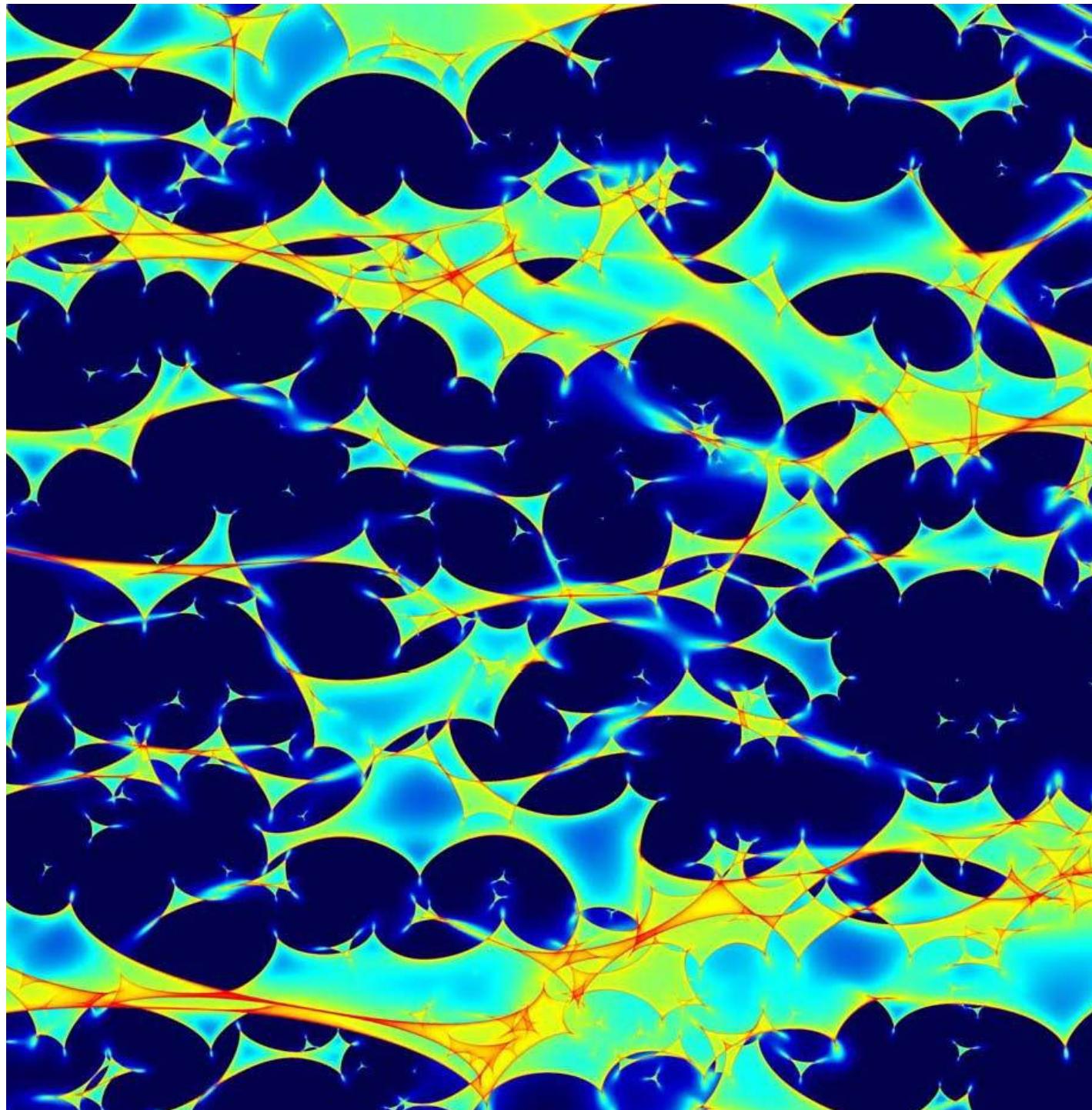
$$k = 0.4$$

$$\gamma = 0.4$$

$$L = 20 R_e$$

Spectral projections $k = 0.4, \gamma = 0.4$



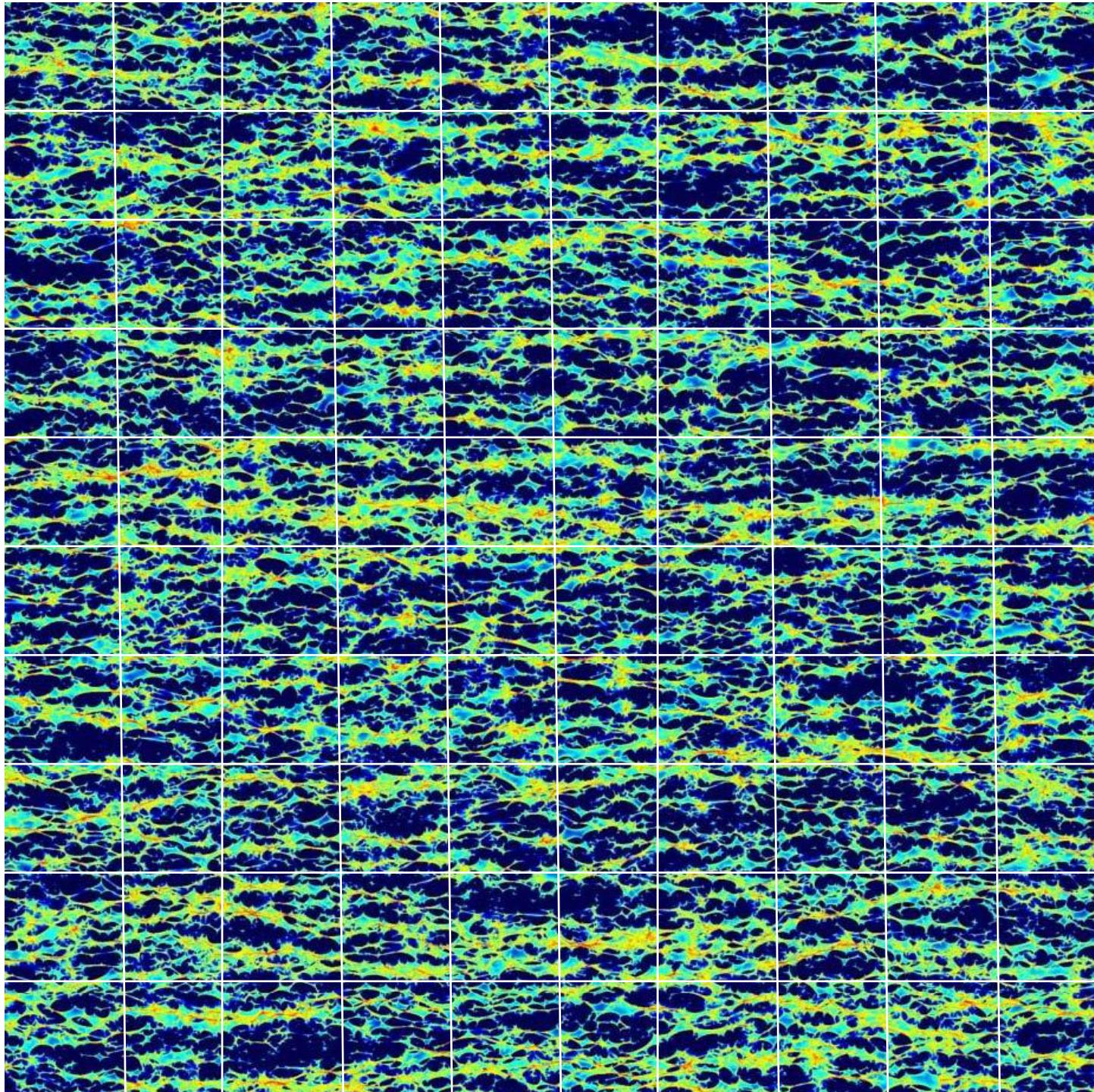


Magnification
pattern

$$k = 0.7$$

$$\gamma = 0.7$$

$$L = 20 R_e$$

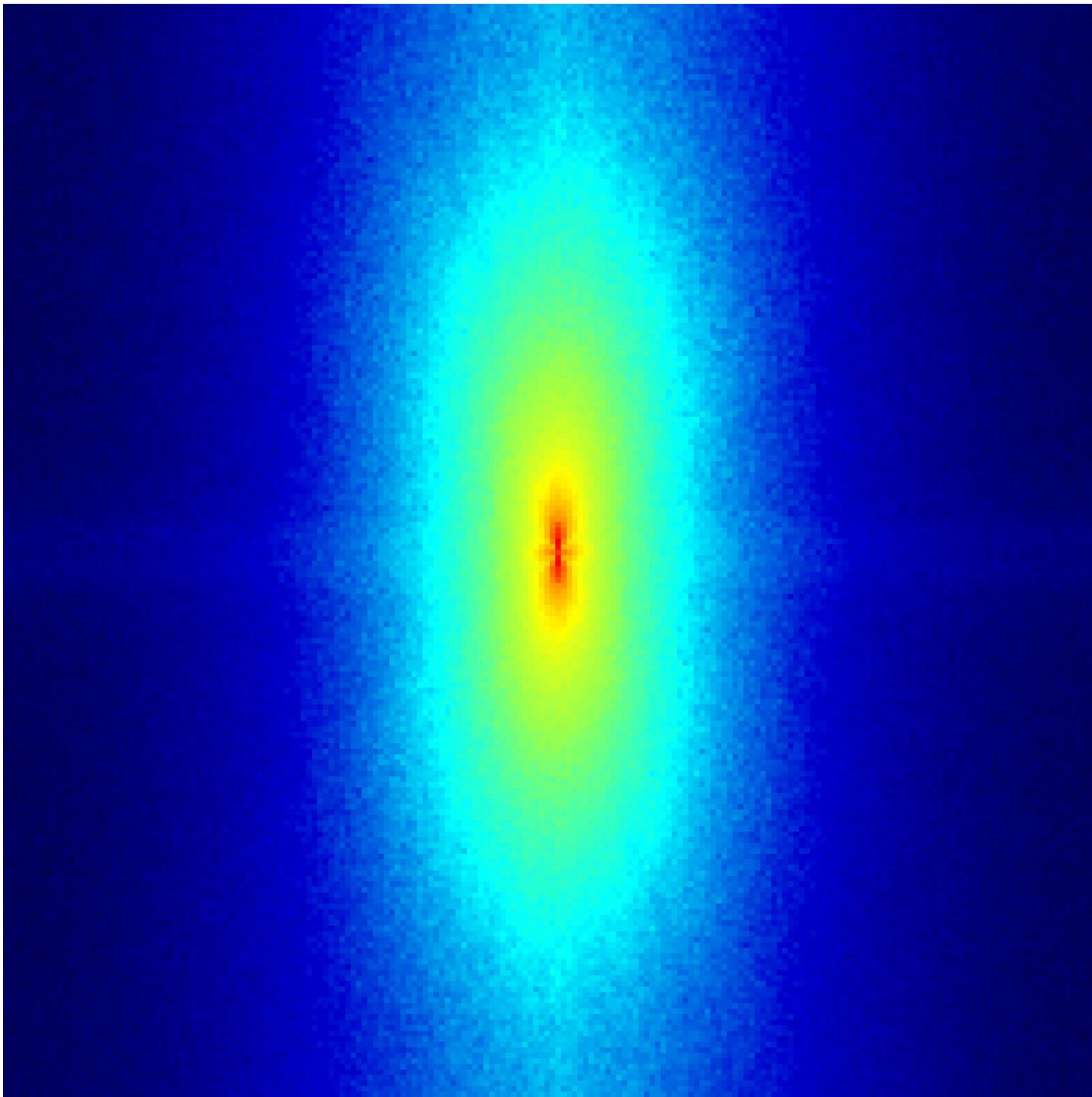


Magnification
pattern

$$k = 0.7$$

$$\gamma = 0.7$$

$$L = 200 R_e$$



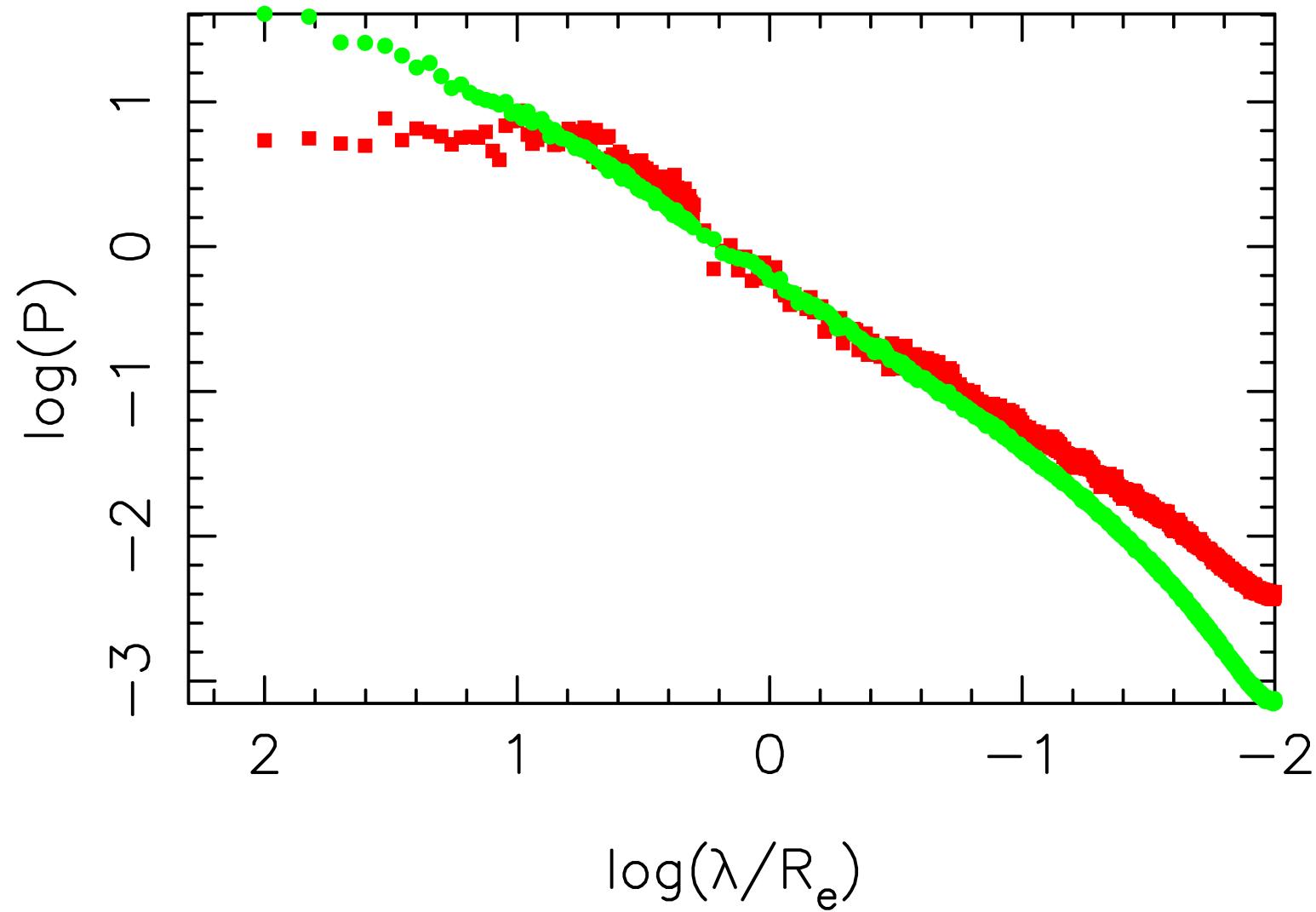
Spectrum

$$k = 0.7$$

$$\gamma = 0.7$$

$$L = 20 R_e$$

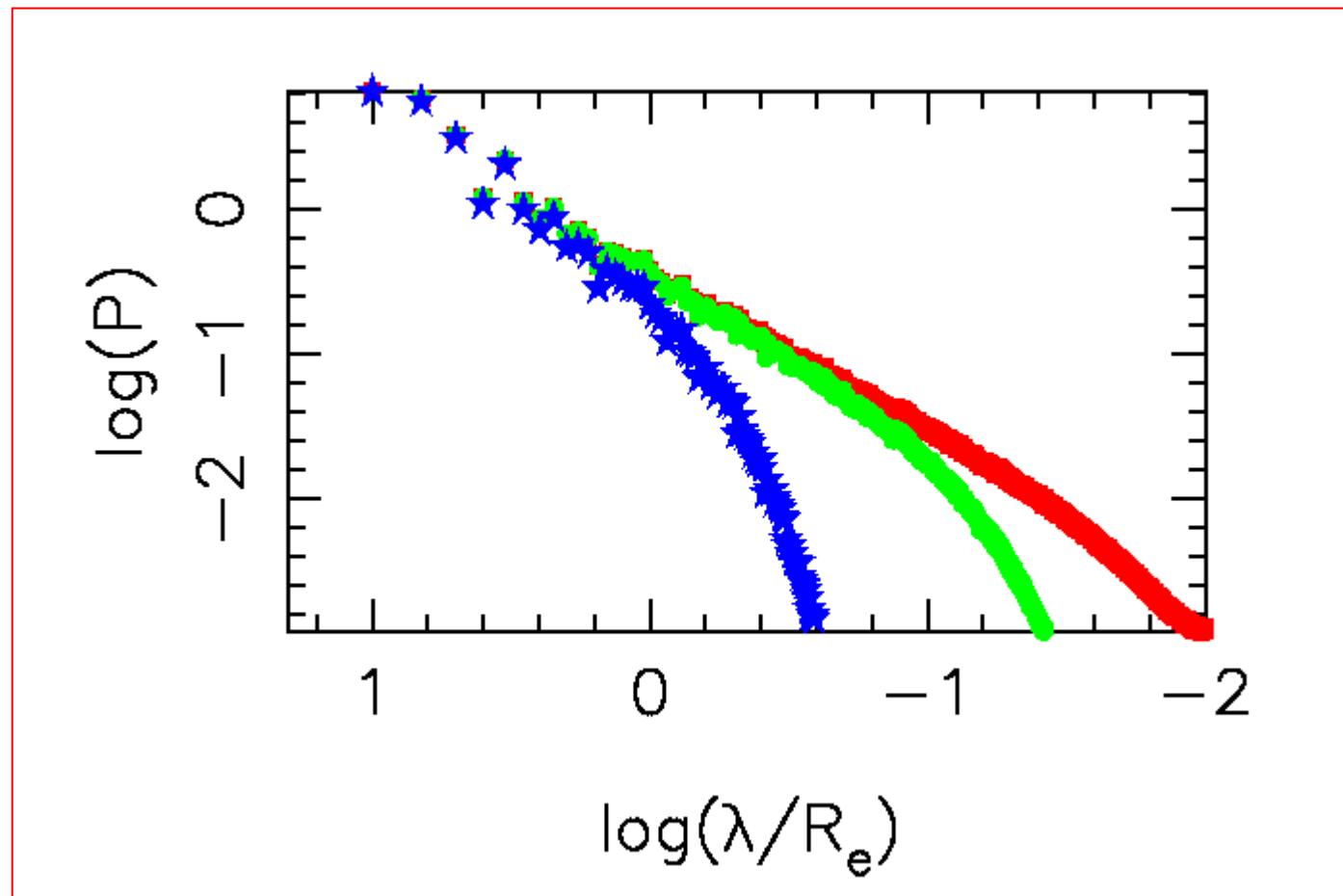
Spectral projections $k = 0.7, \gamma = 0.7$



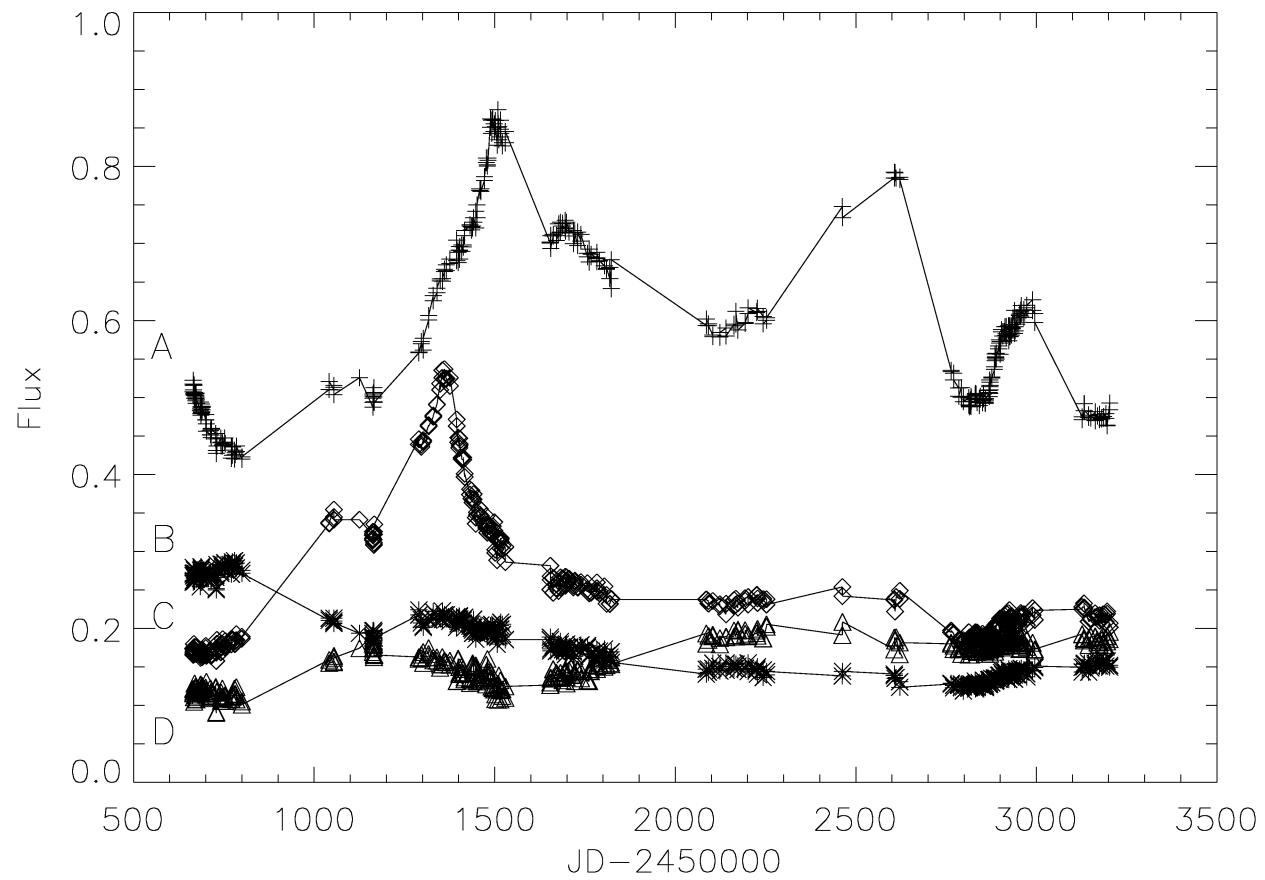
Extended source effect ($k=0.4$, $\gamma=0$, $L=20R_e$)

$$P_{ext}(k) = P_{mag}(k)Q(k) \quad Q(k) : \left| \exp\left[-(R_S k)^2\right] \right|^2 \quad R_S - \text{a source size}$$

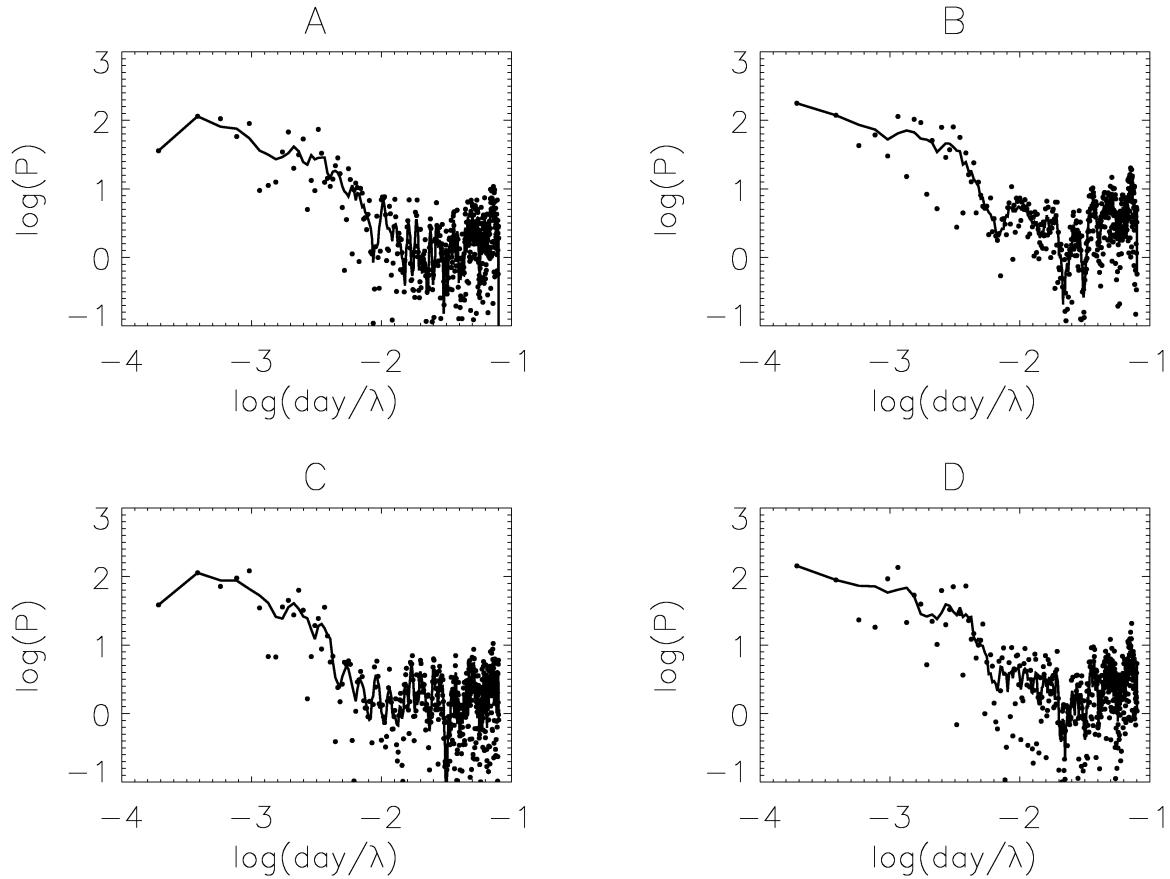
■ - a point source ■ $R_S = 0.01R_e$ ■ $R_S = 0.1R_e$



OGLE monitoring of Q22337+0305



Periodogram of Q2237+0305



Properties of the power spectrum

- a constant at $\lambda \geq 10 R_e$; $\log(\text{day}/\lambda) \leq -3.8$, $\lambda \geq 10^{3.8}$, $R_e \geq 10^{2.8} \approx 600$ days
- a linear decreasing $\sim R_e$;
- a drastic drop at $\lambda \approx 10R_s$; $\log(\text{day}/\lambda) \approx -2.5$, $\lambda \approx 10^{2.5}$, $R_s \approx 10^{1.5} \approx 30$ days